

Methods and Tools for Structural Information Visualization

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Abstract: - In the paper, we consider a practical and general graph formalism called hierarchical graphs and graph models. It is suited for visual processing and can be used in many areas where the strong structuring of information is needed. We present also the Higras, Visual Graph and ALVIS systems that are aimed at supporting of structural information visualization on the base hierarchical graph modes.

Key-Words: - Information visualization, Hierarchical graphs, Hierarchical graph models, Graph algorithm animation, Graph editor, Graph drawing, Graph visualization, Visualization system

1 Introduction

Visualization is a process of transformation of large and complex abstract forms of information into visual form, strengthening user's cognitive abilities and allowing them to take the most optimal decisions.

Graphs are the most common abstract structure encountered in computer science and are widely used for structural information representation [11, 21]. Many graph visualization systems, graph editors and libraries of graph algorithms have been developed in recent years. Examples of these tools include VCG [30], daVinci [7], Graphlet [13], GLT&GET [27], yEd [34] and aiSee [1].

In some application areas the organization of information is too complex to be modeled by a classical graph. To represent a hierarchical kind of diagramming objects, some more powerful graph formalisms have been introduced, e.g. higraphs [9] and compound digraphs [31]. The higraphs are an extension of hypergraphs and can represent complex relations, using multilevel "blobs" that can enclose or intersect each other. The compound digraphs are an extension of directed graphs and allow both inclusion relations and adjacency relations between vertices, but they are less general than the higraph formalism. One of the recent non-classical graph formalisms is the clustered graphs [6]. A clustered graph consists of an undirected graph and its recursive partitioning into subgraphs. It is a relatively general graph formalism that can handle many applications with hierarchical information, and is amenable to graph drawing.

Hence, there is a need for tools capable of visualization of such structures. Although some general-purpose graph visualization systems provide recursive folding of subgraphs, this feature is used only to hide a part of information and cannot help us to visualize hierarchically structural information. Another weak point is that usual graph editors do not have a support for attributed graphs. Though the GML file format, used by Graphlet, can store an arbitrary number of labels associated with graph elements, it is impossible to edit and visualize these labels in the Graphlet graph editor. The standard situation for graph editors is to have one text label for each vertex and, optionally, for each edge.

The size of the graph model to view is a key issue in graph visualization [11]. Large graphs pose several difficult problems. If the number of graph elements is large it can compromise performance or even reach the limits of the viewing platform. Even if it is possible to layout and display all the graph elements, the issue of viewability or usability arises, because it will become impossible to discern between nodes and edges of graph model. It is well known that comprehension and detailed analysis of data in graph structures is easiest when the size of the displayed graph is small. Since none of the static layouts can overcome the problems caused by large graphs, hierarchical presentation, interaction and navigation are essential complements in information visualization.

An algorithm animation visualizes the behavior of an algorithm by producing an abstraction of both the data and the operations of the algorithm [26]. Initially it maps the current state of the algorithm

into an image, which then is animated based on the operations between two succeeding states in the algorithm execution. Animating an algorithm allows for better understanding of the inner workings of the algorithm, furthermore it makes apparent its deficiencies and advantages thus allowing for further optimization.

Applications of graph algorithm visualization can be divided into two types according to the method they implement: interesting events and the data-driven method [4]. Methods of the first type are based on selection of events that occur during execution of an algorithm, for example, comparing the vertex attribute value or removing an edge. Methods of this type create some visual effects for each interesting event. Methods of the second type are based on data changing. During an operation, the memory status is changed, for example, the values of variables. Further these changes are visualized in some understandable way. In the simplest case such changes can be displayed in a form of a table of variable values. This approach is used in debuggers of integrated development environments.

The existing algorithm visualizers have several disadvantages. One of the major drawbacks is that if there is a need to build visualization of an algorithm arbitrarily close to the original algorithm, then it is necessary to build a new visualizer. As a rule, visualizers also do not show the correspondence between the algorithm instructions and the generated visual effects or do not allow reassignment of visual effects to the corresponding events.

In the paper, we consider a practical and general graph formalism called hierarchical graphs and graph models [14]. It is suited for visual processing and can be used in many areas where the strong structuring of information is needed [3, 15, 16, 17, 20, 21, 22, 23, 24, 25, 28, 29]. We present also the Higes, Visual Graph and ALVIS systems that are aimed at supporting of information visualization on the base hierarchical graph modes. The Higes system is a visualization tool and an editor for attributed hierarchical graphs and a platform for execution and animation of graph algorithms [12]. The Visual Graph system was developed to visualize and explore large hierarchical graphs that present the internal structured information typically found in compilers [32]. The ALVIS system was developed to build the algorithm visualization with the help of a flexible system of visual effects and using a visualized graph algorithm as an input parameter.

2 Hierarchical graphs and graph models

2.1 Hierarchical graphs

Let G be a graph of some type, e.g. G can be an undirected graph, a digraph or a hypergraph. A graph C is called a *fragment* of G , denoted by $C \subseteq G$, if C includes only elements (vertices and edges) of G . A set of fragments F is called a *hierarchy of nested fragments* of the graph G , if $G \in F$ and $C_1 \subseteq C_2$, $C_2 \subseteq C_1$ or $C_1 \cap C_2 = \emptyset$ for any $C_1, C_2 \in F$.

A *hierarchical graph* $H = (G, T)$ consists of a graph G and a rooted tree T that represents an immediate inclusion relation between fragments of a hierarchy F of nested fragments of G . G is called the *underlying graph* of H . T is called the *inclusion tree* of H .

A hierarchical graph H is called a *connected* one, if each fragment of H is connected graph, and a *simple* one, if all fragments of H are induced subgraphs of G .

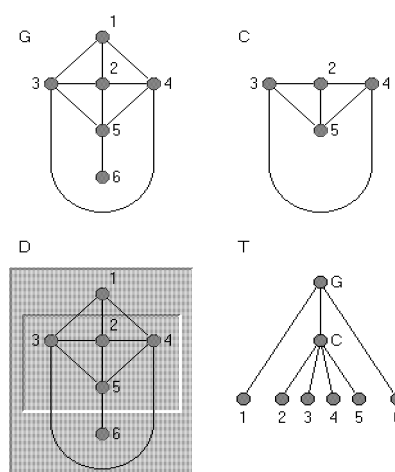


Fig. 1. A simple hierarchical graph $H=(G, T)$ and its drawing D

It should be noted that any clustered graph H can be considered as a simple hierarchical graph $H=(G, T)$, such that G is an undirected graph and the leaves of T are exactly the trivial subgraphs of G (See Fig. 1)

2.2 Hierarchical graph drawing

A *drawing* (or *layout*) D of a hierarchical graph $H = (G, T)$ is a representation of H in the plane such that the following properties hold (See Fig. 1).

- Each vertex of G is represented either by a point or by a simple closed region. The region is defined by its *boundary* - a simple closed curve in the plane.
- Each fragment of G is drawn as a simple closed region which include all vertices and subfragments of the fragment.
- Each edge of G is represented by a simple curve between the drawings of its endpoints.

D is a *structural* drawing of H if all edges of any fragment of H are located inside the region of the fragment. A hierarchical graph is called a *planar* one if it has such a structural drawing that there are no crossing between distinct edges and the boundaries of distinct fragments. The following properties hold.

Theorem 1. There are nonplanar hierarchical graphs $H=(G,T)$ with planar underlying graphs G .

Theorem 2. There are nonplanar hierarchical graphs $H=(G,T)$ having nonstructural planar drawing.

Theorem 3. A simple connected hierarchical graph $H=(G,T)$ is a planar graph if and only if there is such a planar drawing D of G that for any vertex p of T all vertices and edges of $G-G(p)$ are in the outer face of the drawing of $G(p)$.

2.3 Hierarchical graph models

Let V be a set of objects called simple *labels* (e.g. V can include some numbers, strings, terms and graphs). Let W be a set of *label types* of graph elements and let a label set $V(w) = V_1 \times V_2 \times \dots \times V_s$, where $s \geq 1$ and for any i , $1 \leq i \leq s$, $V_i \subseteq V$, be associated with each $w \in W$.

A *labelled hierarchical graph* is a triple (H,M,L) , where H is a hierarchical graph, M is a *type function* which assigns to each element (vertex, edge and fragment) h of H its type $M(h) \in W$, and L is a *label function*, which assigns to each element h of H its label $L(h) \in V(M(h))$.

The semantics of a hierarchical graph model is provided by an equivalence relation which can be specified in different ways, e.g. it can be defined via *invariants* (i.e. properties being inherent in equivalent labelled graphs) or by means of so-called *equivalent* transformations that preserve the invariants.

2.4 Hierarchical control flow graphs

Many problems in program optimization have been solved by applying a technique called *interval*

analysis to the control flow graph of the program [10, 18]. A control flow graph which is susceptible to this type of analysis is called *reducible*.

Let F be a minimal set which includes G and is closed under the following property: if $C \in F$ and p is such an entry vertex of C that subgraph $\{p\}$ does not belong to F then F contains all maximum strongly connected subgraphs of graph which is obtained from C by removing of all edges which are ingoing in p . Let $H_F=(G,T)$ be such a simple hierarchical graph that T represents an immediate inclusion relation between fragments of the hierarchy F .

The following properties hold.

Theorem 4. A control flow graph G is reducible if and only if for the simple hierarchical graph $H_F=(G,T)$ the set of all fragments corresponding vertices $p \in T$ is a hierarchy of nested single-entry strongly connected regions.

Theorem 5. A control flow graph G is reducible if and only if that for any $p \in T$ of the simple hierarchical graph $H_F=(G,T)$ the fragment which is obtained from fragment corresponding to p by reducing all its inner fragments from F into their entry vertices is an interval.

3 The Higes system

3.1 Graph models in Higes

A hierarchical graph supported by the Higes consists of vertices, fragments and edges which we call objects (See Fig. 2). Vertices and edges form an underlying graph. This graph can be directed or undirected. Multiple edges and loops are also allowed.

The semantics of a hierarchical graph is represented in Higes by means of object types and external modules (see below). Each object in the graph belongs to an object type with a defined set of labels. Each label has its data type, name and several other parameters. A set of values is associated with each object according to the set of labels defined for the object type to which this object belongs. These values, along with partitioning of objects to types, represent the semantics of the graph. New object types and labels can be created by the user.

3.2 Visualization

In the Higes system each fragment is represented by a rectangle. All vertices of this fragment and all subfragments are located inside this rectangle.

Fragments, as well as vertices, never overlap each other. Each fragment can be closed or open (See Fig. 2). When a fragment is open, its content is visible; when it is closed, it is drawn as an empty rectangle with only label text inside it. A separate window can be opened to observe each fragment. Only content of this fragment is shown in this window, though it is possible to see this content inside windows of parent fragments if the fragment is open.

Most part of visual attributes of an object is defined by its type. This means that semantically relative objects have similar visual representation. The Higrès system uses a flexible technique to visualize object labels. The user specifies a text template for each object type. This template is used to create the label text of objects of the given type by inserting labels' values of an object.

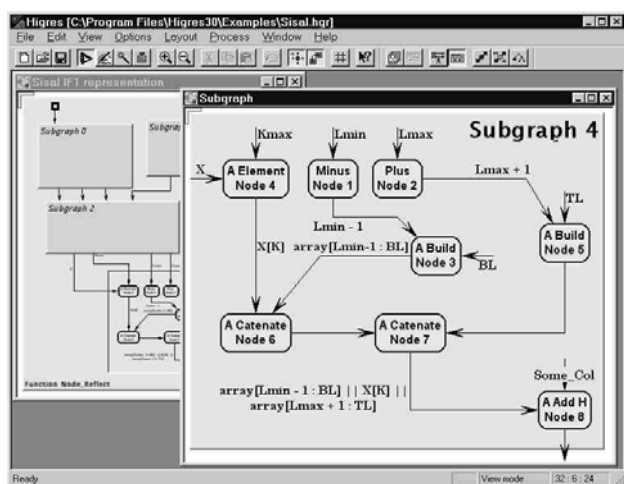


Fig. 2. The Higrès system

Other visualization features include the following:

- various shapes and styles for vertices;
- polyline and smooth curved edges;
- various styles for edge lines and arrows;
- the possibility to scale graph image to an arbitrary size;
- edge text movable along the edge line; colour selection for all graph components;
- external vertex text movable around the vertex; font selection for labels text;
- two graphical output formats;
- a number of options to control the graph visualization.

Now Higrès uses three graph drawing algorithms for automatic graph allocation. The first one is a force method, which is very close to original

algorithm from [5]. The second one is our improvement of the first. The third one allocates rooted trees on layers.

3.3 The user interface

The comfortable and intuitive user interface was one of our main objectives in developing Higrès. The system's main window contains a toolbar that provides a quick access to frequently used menu commands and object type selection for creation of new objects. The status bar displays menu and toolbar hints and other useful information on current edit operation.

The system uses two basic modes: view and edit. In the view mode it is possible only to open/close fragments and fragment windows, but the scrolling operations are extended with mouse scrolling. In the edit mode the left mouse button is used to select objects and the right mouse button displays the popup menu, in which the user can choose the operation he/she wants to perform. It is also possible to create new objects by selecting commands in this menu. The left mouse button can be also used to move vertices, fragments, labels texts and edge bends, and resize vertices and fragments. All edit operations are gathered in a single edit mode. To our opinion, it is more useful approach (especially for inexperienced users) than division into several modes. However, for adherents of the last case we provide two additional modes. Their usage is optional but in some cases they may be useful: the "creation" mode for object creation and "labels" mode for labels editing.

Other interface features include the following:

- almost unlimited number of undo levels;
- optimized screen update; automatic elimination of objects overlapping;
- automatic vertex size adjusting;
- grid with several parameters;
- a number of options that configure the user interface;
- online help available for each menu, dialog box and editor mode.

3.4 Algorithm animation

To run an algorithm in the Higrès system, the user should select an external module in the dialog box. The system starts this module and opens the process window that is used to control the algorithm execution. Higrès provides the run-time animation of algorithms. It also caches samples for the repeated and backward animation. A set of

parameters is defined inside a module. These parameters can be changed by the user at any execution step. The module can ask user to input strings and numbers. It can also send any textual information to the protocol that is shown in the process window.

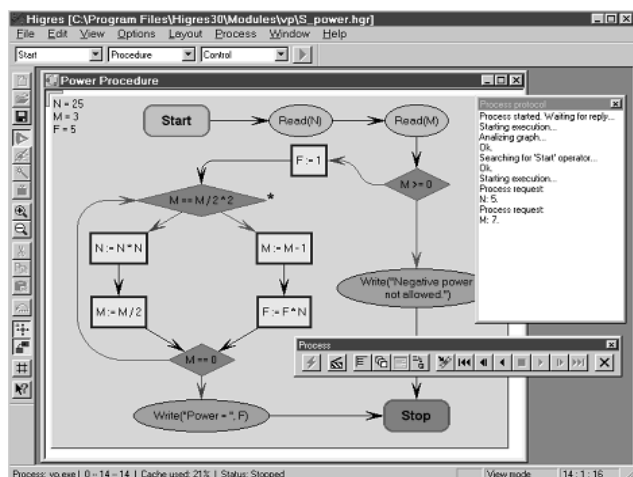


Fig. 3. Simulation of block-scheme representation of a program

A wide range of semantic and graph drawing algorithms can be implemented as external modules. As examples now we have modules that simulate finite automata, Petry nets and imperative program schemes (See Fig.3). The animation feature can be used for algorithm debugging, educational purposes and exploration of iteration processes such as force methods in graph drawing.

A special C++ API that can be used to create external modules is provided. This API includes functions for graph modification and functions that provide interaction with the Higres system. It is unnecessary for programmer, who uses this API, to know the details of the internal representation of graphs and system/module communication interface. Hence, the creation of new modules in the Higres system is a rather simple work.

4 The Visual Graph system

4.1 Visual Graph

Visual Graph is a tool that automatically calculates a customizable multi-aspect layout of hierarchical graph models specified in GraphML (see below). This layout is then displayed, and can be interactively explored, extended and analyzed.

Visual Graph was developed to visualize and explore large graphs that present the internal structured information typically found in compilers.

Visual Graph reads a textual and human-readable GraphML-specification and visualizes the hierarchical graph models specified (See Fig. 4). Its design has been optimized to handle large graphs automatically generated by compilers and other applications.

Visual Graph provides tools for analyzing graph structures. *Structural analysis* means solving advanced questions that relate to a graph structure, for instance, determining a shortest path between two nodes.

Simple possibilities to extend the functionality of Visual Graph (for example, to add a new layout, search, analysis or navigating algorithm, a new tool for processing information associated with elements of graph models and so on) are provided.

4.2 GraphML

GraphML (Graph Markup Language) [2] is a comprehensive and easy-to-use file format for graphs. It consists of a language core (known as the Structural Layer) to describe structural properties of one or more graphs and a flexible extension mechanism, e.g. to add application-specific data. Its main features include support of directed, undirected, mixed multigraphs, hypergraphs, hierarchical graphs, multiple graphs in a single file, application-specific data, and references to external data.

Two extensions, adding support of meta-information for light-weight parsers (Parse Extension) and typed attribute data (Attributes Extension) are currently part of the GraphML specification.

Unlike many other file formats for graphs, GraphML does not use a custom syntax. Instead, it is defined as an XML (Extensible Markup Language) sublanguage and hence ideally suited as an exchange format for all kinds of services generating or processing graphs

4.3 Reducing layout time

Visual Graph was designed to explore large graphs that consist of many hundreds of thousands of elements. However, the layout of large graphs may require considerable time. Thus, there are two main ways to speed up the layout algorithm: multi-aspect layout of graph and control of layout algorithms.

The first way in visualizing a large graph is aimed at avoiding computing the layout of parts of the graph that are currently not of interest. Interactive exploring of graph is based on step by step construction of so-called *multi-aspect layout* of

graph being a set of drawings of some subgraphs of the graph. For presentation of multi-aspects layout a set of windows which includes a separate window for visualization of each considered subgraph is used. At each step of the construction a layout algorithm is applied to a subgraph being interested to user at this step. To indicate the interested subgraph the user can select its elements in the active window or in the navigator (see below). The user can also define some condition in the filter or in the search panel (see below). Then the condition will be used for searching of graph elements which will form the interested subgraph. The search can be performed both locally (in some part of graph, e.g. through a subgraph presented in the active window) or globally (around the entire graph). Multi-aspect drawing of graph models makes every visible part of the graph smaller, thus enabling the layout to be calculated faster and the quality of the layout to be improved.

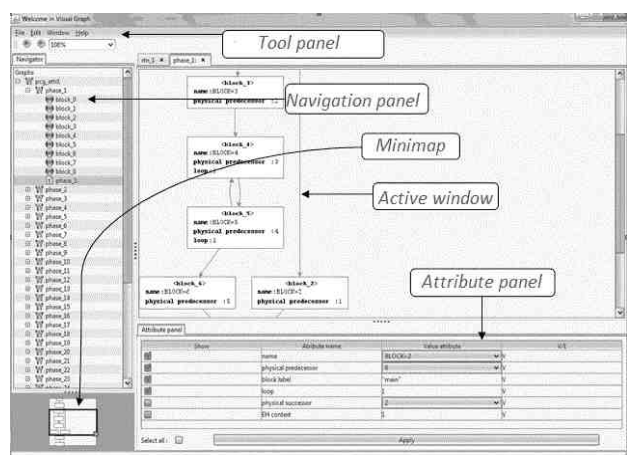


Fig. 4. The Visual Graph system

In order to further reduce layout time, it is possible to control the layout algorithms, e.g. some layout phases can be omitted or the maximum number of iterations of some layout phases can be limited. However, this usually decreases the quality of the layout. The user can improve the layout by hand, e.g. by moving of nodes or changing of their sizes or forms.

4.4 Navigating through a graph

Visual Graph offers several tools for navigating through a graph model: minimap, navigator, attribute panel, filter, search panel, notebook.

The *minimap* visualizes a *working region* of the graph model explored (See Fig. 4). It shows both the whole subgraph from the active windows and its visible part (i.e. such a subgraph part that is

allocated in the active window). It is possible to change both the visible part of the subgraph from the working region and scale of its drawing.

The *navigator* visualizes inclusion trees of hierarchical graph models as hierarchies of their vertices. It is possible to open in the active window any vertex of any group of vertices.

The *attribute panel* allows for elements of graph model in the working region choose attributes which should be visualized and ways of their visualization.

The *filter* is used for searching such elements of graph in the working region which satisfy given conditions (See Fig. 5).

The *search panel* is intended to search such elements of either whole graph model or its given part which satisfy given conditions.

The *notebook* can load files with additional information (e.g. with a source program being compiled) and associate it with graph elements.

5 The ALVIS system

5.1 Interactive visualization model

A new algorithm visualization model based on the dynamic approach and hierarchical graph models has been created. The main point of the suggested model is that the given algorithm is formulated in some programming language that allows us to use instructions operating with graphs and to execute the program derived from the text of the algorithm after a set of transformations. More details about the model can be found in [8]. The result of the program execution is information which is to be used in creation of the underlying algorithm visualization. An example of such instruction can be adding an edge or a change in the attributes of vertices. The following example shows the breadth-first search algorithm for any graph. In the given case, *Get* and *Set* instructions are used for reading and changing the graph element's attribute values. These instructions have formats *Get(Vertex, AttributeName)* and *Set(Vertex, AttributeName, AttributeValue)*, respectively. To construct a visualization of the breadth-first search algorithm, the state attribute is appointed to each graph vertex. The value of the state attribute reflects whether the vertex was visited during graph traversal.

```
VertexQueue.Enqueue(Graph.Vertices[0]);
while (VertexQueue.Count > 0)
```

```

{
Vertex v = VertexQueue.Dequeue();
Set(v, "state", "visited");
foreach(Edge e in v.InEdges)
{
Vertex t = e.PortFrom.Owner;
string c = Get(t, "state");
if(c != "visited")
{
Set(t, "state", "visited");
VertexQueue.Enqueue(t);
}
}
}
foreach(Edge e in v.OutEdges)
{
Vertex t = e.PortTo.Owner;
string c = Get(t, "state");
if(c != "visited")
{
Set(t, "state", "visited");
VertexQueue.Enqueue(t);
}
}
}
VertexQueue.Clear();

```

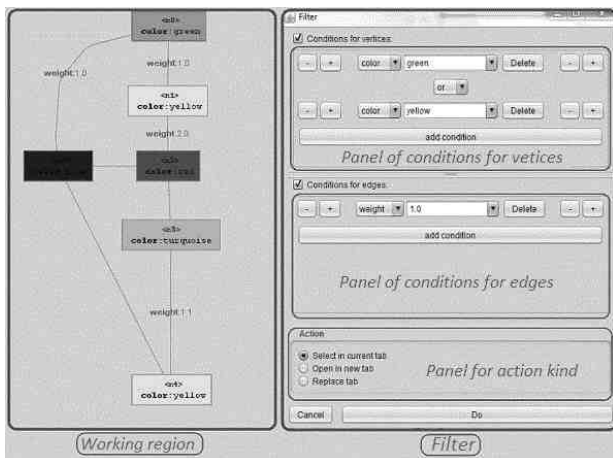


Fig. 5. The filter of the Visual Graph system

Each instruction of the algorithm generates one or more images of the current state of the graph model. The graph model is an annotated hierarchical marked graph. It is useful to highlight the current executing instruction in each image because it allows a user to keep attention on valuable events at this moment. To solve the problem of highlighting the current executing instruction in the image, the following approach is used. Each text line of an algorithm can be

interpreted as a function. Also, each text line has a numeric index in all text lines. So that order value is added to arguments of the function corresponding to the text line. This additional parameter is the number of the current executing algorithm instruction. After this transformation, the text of the breadth- first search algorithm from the above example looks like this:

```

VertexQueue.Enqueue(Graph.Vertices[0]);
while (WhileCondition(2, VertexQueue.Count > 0))
{
Vertex v = VertexQueue.Dequeue(3);
Set(4, v.ID, "state", "visited");
foreach(Edge e in ForeachCollection(5, v.InEdges))
{
Vertex t = e.PortFrom.Owner;
string c = Get(7, t, "state");
if(If Condition(8, c != "visited"))
{
Set(10, t, "state", "visited");
VertexQueue.Enqueue(11, t);
}
}
}
foreach(Edge e in ForeachCollection(13, v.OutEdges))
{
Vertex t = e.PortTo.Owner;
string c = Get(16, t, "state");
if(If Condition(17, c != "visited"))
{Set(19, t, "state", "visited");
VertexQueue.Enqueue(20, t);
}
}
}
VertexQueue.Clear( );

```

The above example shows changes in the attributes of the graph elements, too. This is a typical situation for algorithms implementing only traversal of a graph - a method when all graph vertices are visited one by one. For example, the Prüfer sequence of a given tree is generated by iteratively removing vertices from the tree until only two vertices remain. To perform this operation, the *RemoveVertex()* instruction should be used, which leads to generation of a visual effect of the corresponding vertex disappearing. Here is an example of the Prüfer encoding algorithm, how it can be formulated as a parameter of the graph algorithm visualization system:

```

int i = 0;
List<Vertex> Leafs = new List<Vertex>( );
int n = Graph.Vertices.Count;
while(i++ <= n-2)
{
Leafs.Clear();
foreach(Vertex v in Graph.Vertices)
if(v.OutEdges.Count == 0) Leafs.Add(v);
Vertex codeItem =
Leafs[0].InEdges[0].PortFrom.Owner;
Output.Add(codeItem);RemoveVertex(Leafs[0]);
}

```

Each algorithm instruction generates some information during execution of the transformed text of the original algorithm. This information describes the number of the current instruction, the name of an attribute of a graph element, the previous value of the attribute, a new value of the attribute and the identifier of the graph element. This information allows us to get the full log of operations executed over graph elements. This operation log contains the detailed information on the state of the graph model during the algorithm running. Further the log of operations, the input graph and the original text of the algorithm can be used to generate the algorithm visualization. Each operation log entry corresponds to some graphical effect over visual representation of graph elements. The simplest example of the visual effect for the breadth-first search algorithm is to change the color of the graph vertex representation when a state attribute of the vertex has been changed and to change the color of the text of the corresponding instruction.

5.2 Algorithm visualization system

The ALVIS system for graph algorithm visualization on the base of the described model has been constructed.

The system includes two main components: an algorithm execution module and a graph algorithm visualizer. It is assumed that data are passed between these and other components of the system in a text form. It means that components of the system can be implemented on different platforms and with different tools.

The purpose of the algorithm execution module is to generate the execution log. The algorithm running is separated from its visualization. This allows us to perform the algorithm once and after that the operation log can be used to visualize and refine the visualization many times. This can be useful when computationally-intensive algorithms

are visualized. In such cases the second cycle of execution of the algorithm is complex.

To provide correct work of the algorithm execution module, it is necessary to meet a significant condition. Since any existing compiler or interpreter can be used to create this module, the algorithm must be formulated in the language supported by the selected compiler or interpreter. Actually this is not a restriction on the algorithm implementation language since many programming languages allow graph structures to be used in the program source code. So, the given algorithm text can be considered as a ready program source code. Also this allows us to transmit the input graph in this compiled program and to generate the log of operations.

Another significant restriction relates to the algorithmic complexity. In this approach, it is reasonable to visualize only efficient algorithms, because it will take much time to build the operation log of execution of an efficient algorithm. We can use a small input graph for this case. This assumption allows us to construct visualization for a reasonable time.

The algorithm execution module takes the given algorithm text in an appropriate programming language, executes it and returns the log of operations generated during the algorithm run on a particular graph. The log of executed operations contains information about all changed attributes of graph elements and about graph elements added or removed during the execution. Further this information is used to generate the algorithm visualization.

Another main component of the ALVIS system is the graph algorithm visualizer. At its input, this component receives the algorithm text, the input graph, the log of operations and additional graphical options. A log information item is added by special instructions created at the stage of preparation of the algorithm text. For example, these special instructions are the functions: *Set()*, *Get()*, *IfCondition()*, *WhileCondition()* and *ForeachCollection()*. Their first argument is the number of the corresponding text line. *IfCondition()* and *WhileCondition()* do not perform any changes in the graph model state but at least allow us to make a visual selection of the text line where it was inserted. *ForeachCollection()* is to be used to generate information which allows highlighting a set of vertices before they will be actually enumerated. To add these functions into appropriate places of the original algorithm, it is sufficient to use a contextual replacement. The purpose of the preparation stage is to eliminate the

need for declarative structures, which have no relation to the actual nature of the algorithm.

A log item may also contain information about the value of an attribute of a graph element. A graph element is a vertex, an edge or a port. If there is a vertex with its incident edge, then a port is a point where the edge enters the vertex. When rendering, it can be useful that the points are allocated for these additional objects. Ports simplify calculation of coordinates of graphical primitives which represent the edge elements. Strictly mathematically, it is possible to simulate a port with a labeled vertex. So the class of graphs with ports is isomorphic to the class of all graphs.

An attribute of a vertex, an edge or a port can have a string name and a string value. The log of operations stores the previous value of the attribute for a particular graph element. This information is also useful for building the visualization, since it is possible to make a smooth visual effect from a previous value of an attribute to its new value.

It is not obvious how to bind information from a log item to the visual effect. In this case, a user needs to interfere in order to set an explicit binding between the set of attributes in the text of the algorithm and the desired visual effects. For example, if the operation of a log item is about changing the coordinates of the graph element reflected with the use of the attribute "position", then it is reasonable to bind the attribute with the visual effect, which leads to a shift of the graph element. Another user example is to bind all log items to the effect of a color mark of a current graph element under processing. It can be a current vertex visited in the algorithm of depth-first search or in any other graph traversal. In this aspect the suggested approach is close to the interesting events approach, where an algorithm instruction is an interesting event.

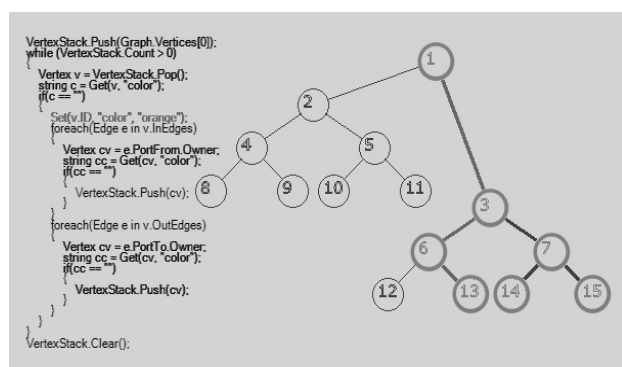


Fig. 6. Visualization of the depth-first search algorithm

Fig. 6 shows an example of visualization of the depth-first search algorithm on the graph, which is actually a binary tree. It is one of the screenshots taken during the process of visualization of the depth-first search algorithm. The left side of the figure displays the text of the algorithm formulated in terms of graph operations. The attribute of a graph vertex indicates the fact that the vertex has already been visited during the process of the graph traversal. A line of the algorithm text has one of the following states: dark thin, light thin and thick. The first state means that the instruction has been executed at least once. The second state means that the current image and the last shown visual effect is the result of this instruction. The last state means that the instruction has not been executed yet. The right part of the figure displays the graph model, which is a hierarchical graph with attributes. Only if this attribute is set, the corresponding attribute will be created during visualization. In this example, the visited vertices get the state attribute that changes the color of a vertex. Also, this attribute's value corresponds to the increase of line width showing the graph vertex circle. Vertices shown in a thin line have not been visited yet.

Displaying of additional data structures can also be used to improve understanding of visualization of a graph algorithm. For example, the depth-first search algorithm uses a stack and the breadth-first search algorithm visualization uses a queue. The content of a stack or a queue can be represented as a graph. Since the visualization system allows us to use the hierarchical graphs, a stack graph or a queue graph can be included into a graph model for a particular visualization. So the working graph model consists of a graph with two vertices. The first vertex contains a stack graph and the second contains an input graph. Such graph model can be visualized with the created module of the system of graph algorithm visualization. The queue or stack size is changed during execution of the given algorithm and the corresponding vertices are added or removed from the stack graph. Hierarchical graphs are helpful for this purpose. If there is no stack or queue, then a tree of fragments only consists of one fragment, the input graph. For a stack the graph model consists of three fragments: a root and two children. The first child is the input graph and the second is a graph representation of the stack. So, if the given algorithm uses an input graph and N additional structures, then the tree of fragments contains $N+2$ elements. It is a root element and its $N+1$ children,

one of which is the input graph and others are graph representations of additional data structures.

6 Conclusion

In the paper, a practical and general graph formalism of hierarchical graphs and graph models was considered. It is suited for visual processing and can be used in many areas where the visualization of structural information is needed

The Higes system being a visualization tool and an editor for attributed hierarchical graphs and a platform for execution and animation of graph algorithms was presented. The Visual Graph system intended to visualize and explore large hierarchical graphs that present the internal structured information typically found in compilers was considered. The ALVIS system which builds the algorithm visualization with the help of a flexible system of visual effects and using a visualized graph algorithm as an input parameter was described.

The described methods and systems will be used in Web-Encyclopedia of Graph Algorithms (WEGA) [33] which is under development on the basis of our book [19] and is aimed to be not only a reference manual on graph algorithms but also an introduction to the graph theory and its applications to computer science.

In contrast to Donald Knuth who used the assembly language of the so-called MIX computer in his fundamental books “The art of computer programming”, we decided to use a high-level and language-independent representation of graph algorithms in our book and system. In our view, such an approach is preferential, as it allows us to describe algorithms in a form that admits direct analysis of their correctness and complexity, as well as a simple translation of algorithms to high-level programming languages without disturbance of their correctness and complexity. Besides, the described approach allows the readers to understand an algorithm at the informative level, to evaluate its applicability to a specific problem, and to make all its modifications needed for correct application of the algorithm.

We also believe that visualization could be very helpful for readers in understanding graph algorithms, and we plan to embed capabilities of interactive animation of graph algorithms which will be described into the WEGA system.

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