# **Cooperative Spatial Multiplexing for CR Users Sharing a Common Channel with Primary Users**\*

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Abstract: To enable mobile stations (MSs) of secondary users (SUs) in cognitive radio (CR) networks sharing a common channel with MSs of primary users (PUs) is an important but challenging issue. In this paper, a cooperative spatial multiplexing (CSM) scheme is proposed, where base station (BS) in CR network has K antennas and each SU or PU has one antenna only, and BS supports PUs and SUs by K spatial channels. To ensure communication quality of the network, the paper applies LDPC as the channel coding for BS, PUs and SUs. Simulations verify the proposed scheme with good spatial multiplexing capacity and BER performance.

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# 1. Introduction

The demand for high data rates in wireless networks significantly increased over the last few years and stimulated the interest in efficient utilization of so called multiple-input multiple-output systems (MIMO) [1-19]. By utilizing multiple antenna architectures at both BS and MSs of CR network, significantly higher channel capacities close to that of wired networks are possible [1, 2, 16-19]. While, there are two problems need to be solved: first one is co-channel interference for SUs' and PUs' in a network, since SUs' and PUs' channels are not sure to be orthogonal each other; second one is MSs implementation complexity [16-19]. In the uplink, sophisticated multiuser detection (MUD) can be implemented at the BSs to counter the co-channel interference, however in the downlink, the MS receivers are usually required to be simple. In particular, in broadcast scenarios (downlink situation), where no joint processing of the received signals is possible, MIMO precoding schemes in [4, 5] are attractive since they can be viewed as the counterpart to successive cancellation which is applicable in uplink scenarios only.

Different from classical MIMO, the existing cooperative spatial multiplexing (CSM) schemes for MIMO network [10-15] need several base stations (BSs) and mobile stations (MSs) to support one data transmitting. However, there are four vital problems for this scheme to hinder CSM's application. The first problem is the exact synchronization among the MSs and BSs; the second one is the spatial channels' estimation for BSs and MSs [20]. The third one is space-time coding and decoding for the BSs and MSs, every one of the MSs and BSs needs to know the spatial channels' parameters [16, 20]; and the fourth one is the complexity of the implementation systems and MIMO network. That is to

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say, we can not follow the existing CSM schemes [10-15], and had to propose new CSM solutions. The proposed CSM systems including the MIMO base stations (BS) and MIMO MS are designed, while we can not apply the existing CSM schemes [10-15] simply because of the above problems.

The proposed cooperative spatial multiplexing systems in this paper are different from the existing CSM schemes [10-15]. First, in our CSM, one CR network has one BS and many MSs of (PUs and SUs), BS has K antennas, while each MS only has one antenna, MSs have not used MIMO technique: no space-time coding and decoding. Second, in the proposed scheme, the CSM provides the BS of K antennas to support K MSs by one frequency channel only, the existing CSM schemes have not considered our approach. Third, the proposed CSM scheme solves the co-channel interference in CR network by LDPC [21-25], but the existing CSM schemes have no ability to solve the problem. Fourth, there is the synchronization problem among the MSs and BSs of the existing CSM schemes, one BS can support K MSs with independent spatial channels. Fifth, contrary to the existing CSM, in the proposed CSM, MSs need not to estimate the spatial channels' parameters, which make their implementation simplified greatly.

The following contents are organized as following. The proposed CSM downlink and CSM uplink schemes based on MIMO-CR network are given in Section II and Section III, respectively. In Section IV, we give the simulation results of a MIMO-CR network. Finally, Section V concludes the paper.

# 2. The Proposed Csm Downlink of Mimo-cr Network

Consider the downlink channel of MIMO-CR network shown in Fig. 1. In the proposed MIMO CR systems, the BS

in CR network uses K antennas to transmit and receive the MSs' data stream of real symbols. From Fig.1, we see that the K downlink paralleled sequences for K MSs are transmitted from K antennas of BS transmitter. Since BS has K antennas, BS can divide K MSs into SU group and PU group who share the same frequency bandwidth in CR network.

In Fig.1, to keep the MIMO channels be independent, the distance of two MSs is lager than 10 radio signal wavelengths, and the distance of two receiving antennas of BS is lager than 4 radio signal wavelengths, else the channel matrix may be singular.

The proposed CSM scheme in Fig. 1 can provide K spatial channels to support K MSs of PUs and SUs at one frequency band-width, while there is one PU only for existing CR network only at one frequency band-width, and all SUs had to back-off.



Fig. 1 The downlink channel of MIMO-CR network

We consider using MIMO precoding at the transmitter MIMO-CR BS, the purpose is to simplify the receiver implementation of MSs of PUs and SUs. The implementation complexity of proposed MIMO-CR systems is moved to BSs: downlink MIMO ZF precoding, so there is no space-time coding and decoding for MSs of PUs and SUs.

The proposed BS transmitter structure supports spatial multiplexing scheme for downlink transmission, and it is shown as in Fig. 2. In the proposed MIMO-CR network, MSs need not estimate the MIMO channel parameters, and they only need to provide BS an uplink pilot for k th time-slot.



Fig. 2 MIMO precoding transmitter of BS for MSs

Fig. 2 only provides base-band processing blocks of the BS transmitter. Considering K MSs, the BS transmitter include K processing blocks as that in Fig.2. BS can determine the spatial multiplexing number by the number of PUs and MUs.

At downlink, firstly, BS's LDPC codec encodes the MSs data streams  $\{u_1^{(k)}\}$ , ...,  $\{u_K^{(k)}\}$  of k th time-slot into K streams  $\{b_1^{(k)}\}, ..., \{b_K^{(k)}\}$  for MS<sub>1</sub>,..., MS<sub>K</sub>.

Secondly, the LDPC streams  $\{b_1^{(k)}\}, ..., \{b_K^{(k)}\}$  of MSs are precoded by inversed channel matrix as a linear combination of the K sub-streams  $s_1^{(k)}, ..., s_K^{(k)}$ ,

$$\begin{bmatrix} s_{1}^{(k)} \\ \vdots \\ s_{K}^{(k)} \end{bmatrix} = \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix}^{-1} \begin{bmatrix} b_{1}^{(k)} \\ \vdots \\ b_{K}^{(k)} \end{bmatrix}$$
(1)

where  $h_{ij}^{(k)}, i, j \in \{1, ..., K\}$  denote the channel coefficient that the path from the transmitter antenna *i* to the MS's antenna *j* experiences independent Rayleigh fading, shown in Fig.1, and we let

$$\mathbf{H}_{(k)} = \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix}$$
(2)

In the proposed BS system, the channel parameters of  $\mathbf{H}_{(k)}^{-1}$  are provided by the channel estimation model of BS, shown in Fig.2.

BS in the proposed scheme accesses the MSs according to the spatial channels to be independent for the K MSs, which requires  $\mathbf{H}_{(k)}$  should be full rank. This is always possible since the number of active MSs at different positions in CR network is always larger than K. The BS only does not select the MSs to be near each other [16].

In the proposed scheme, we need not require the MSs to estimate the channel parameters, since it will greatly increase the implementation complexity of MSs. The channel estimation is arranged on BS utilizing the approach of [9].

The received signals at the antennas of MSs are given by

$$\begin{bmatrix} r_{1}^{(k)} \\ \vdots \\ r_{K}^{(k)} \end{bmatrix} = \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix} \begin{bmatrix} s_{1}^{(k)} \\ \vdots \\ s_{K}^{(k)} \end{bmatrix} + \begin{bmatrix} n_{1}^{(k)} \\ \vdots \\ n_{K}^{(k)} \end{bmatrix}$$
(3)

where  $h_{ij}^{(\kappa)}, i, j \in \{1, ..., K\}$  denote the channel coefficient that the path from the transmitter antenna *i* of BS to the receiver antenna of MS *j* experiences independent Rayleigh fading. The receiver noises  $n_i^{(k)}, j \in \{1, ..., K\}$  of the antenna j are normalized to be CN(0,1) (zero-mean unit-variance complex Gaussian).

Since the precoding at BS is adopted, the received signals  $r_i^{(k)}$ , i = 1, ..., K, from the MSs' antennas, are independent, and can be further written as

$$\begin{bmatrix} r_{1}^{(k)} \\ \vdots \\ r_{K}^{(k)} \end{bmatrix} = \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix} \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix}^{-1} \begin{bmatrix} b_{1}^{(k)} \\ \vdots \\ b_{1}^{(k)} \\ \vdots \\ b_{K}^{(k)} \end{bmatrix} + \begin{bmatrix} n_{1}^{(k)} \\ \vdots \\ n_{K}^{(k)} \end{bmatrix}$$
$$= \begin{bmatrix} b_{1}^{(k)} \\ \vdots \\ b_{K}^{(k)} \end{bmatrix} + \begin{bmatrix} n_{1}^{(k)} \\ \vdots \\ n_{K}^{(k)} \end{bmatrix}$$
(4)

From (4), the proposed MS receiver can be very simple, whose base-band circuit is shown in Fig.3. The soft information  $r_i^{(k)}$  needs to be decoded by LDPC decoder in Fig.3 [21-25].



Fig. 3 The MS receivers of MIMO CR network

The proposed CSM downlink scheme of MIMO CR system, the MSs need not estimate the spatial channel parameters, the base station of CR network provides K spatial channels for K MSs. This is one of main contributions of the proposed CSM scheme. However, in the downlink of wireless network, the existing CSM receivers need to joint-recover the transmitted data streams from BS by channel matrices, and MSs had to estimate Rayleigh channel parameters by the pilot signals of BS [10].

## 3. The Proposed Csm Uplink of Mimo-cr Network

Considering the uplink of the CSM MIMO-CR network shown as in Fig.4, where there are K antennas at BS but there is one antenna of at each MS, assuming there are K active MSs in the network. The MSs transmit the K streams through its single transmitting antenna through the flat fading channels in the MIMO-CR network. The proposed BS assigns spatial channels to the MSs of PUs and SUs according to their spatial positions, and MSs should not near each other.

The proposed MS transmitter of MIMO-CR network is shown in Fig.5. At the uplink, firstly, MS's LDPC codec encodes its data streams  $\{u_i^{(k)}\}, i = 1, ..., K$  into LDPC

streams  $\{b_i^{(k)}\}, i = 1, ..., K$  [21-25]. Then, the LDPC streams are transmitted different MSs, and they are received through Rayleigh fading channel by BS.





Fig.5 The MS transmitter of MIMO-CDMA network

Different from the existing CSM schemes for MSs, from Fig.5, we see that the proposed MS transmitter has no space-time coding. The CSM gain is obtained by the proposed BS MIMO receiver.

The proposed MIMO-CR BS receiver K MSs is shown in Fig. 6. In the proposed CSM scheme, each MS provides an uplink pilot sequence to BS. BS obtains the spatial channel parameters by the MS's pilot [9], this is different from the other existing CSM scheme.



Fig. 6 MIMO receiver of MIMO-CD BS

The received signals at K antennas of BS are given by

$$\begin{bmatrix} r_{1}^{(k)} \\ \vdots \\ r_{K}^{(k)} \end{bmatrix} = \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix} \begin{bmatrix} b_{1}^{(k)} \\ \vdots \\ b_{K}^{(k)} \end{bmatrix} + \begin{bmatrix} n_{1}^{(k)} \\ \vdots \\ n_{K}^{(k)} \end{bmatrix}$$
(5)

where  $h_{ij}^{(k)}$ ,  $i, j \in \{1, ..., K\}$  denote the channel coefficient that the path from the MS *i* to the receiver antenna *j* of BS experiences independent Rayleigh fading. The receiver noise

vectors  $n_j^{(k)}$ , j = 1, ..., K of the antenna j are normalized to be CN(0,1) (zero-mean unit-variance complex Gaussian).

From  $r_i^{(k)}$ , i = 1, ..., K, the MIMO decoding model

recovers  $\{z_i^{(k)}\}, i = 1, ..., K$ , the LDPC coded streams with channel noise by using  $\mathbf{H}_{(k)}^{-1}$ ,

$$\begin{bmatrix} z_{1}^{(k)} \\ \vdots \\ z_{K}^{(k)} \end{bmatrix} = \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix}^{-1} \left( \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix}^{-1} \left( \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{1K}^{(k)} \end{bmatrix}^{-1} \begin{bmatrix} n_{1}^{(k)} \\ \vdots \\ n_{K}^{(k)} \end{bmatrix} + \begin{bmatrix} h_{11}^{(k)} & \dots & h_{1K}^{(k)} \\ \vdots & \ddots & \vdots \\ h_{K1}^{(k)} & \dots & h_{KK}^{(k)} \end{bmatrix}^{-1} \begin{bmatrix} n_{1}^{(k)} \\ \vdots \\ n_{K}^{(k)} \end{bmatrix}$$
(6)

where  $z_i^{(k)}$ , i = 1, ..., K need to be decoded into  $u_i^{(k)}$ , i = 1, ..., K by LDPC decoder of the BS [21-25], which is shown in Fig.6.

#### 4. Simulations

We assume that in a MIMO-CR network, there are one BS and four MSs (one is PU, three are SUs), BS has 4 antennas, and each MS has one antenna only, BS obtains the perfect channel estimation by the approach of [9], and the transmitted signals are modulated by BPSK.

To verify the LDPC role [21-25] in the proposed CSM system of MIMO-CR network to be valid, we simulate the downlink and uplink of MIMO-CR network with LDPC in MIMO-CR network. In following two experiments, we use the same QC LDPC codes in [21], in our system simulation, p = 127, a = 2 and b = 7. Thus, the QC code has the code rate 1/2, and code length to be 1270.

**Experiment 1:** BER simulation of the proposed downlink MIMO-CR system with LDPC. BS had to use the proposed CSM to let one frequency band-width to support one PU and three SUs.

In the downlink network's simulation, the two systems (one with LDPC, the other no) transmit 200 data frames under same SNR and channel conditions, where

H=	0.9	0.31	0.29	0.13	
	0.19	0.78	0.4	0.21	
	0.24	0.3	0.71	0.33	
	0.11	0.17	0.4	0.83	

The obtained BER results are shown in Fig. 7. Observing simulation results in Fig.7, we find that the PU and SUs have similar BER performance at MIMO-CR downlink, if BS has perfect channel estimation. When SNR is larger than 6, the BER of PU and SUs is smaller than  $10^{-5}$ , which is expected by us. From (4), we also know that the precoding algorithm

can complete the spatial separation for K MSs' data screams. For the MSs, the received data is independent each other, and the multiuser interference has been removed due to (4).



Fig. 7 The bit error rates (BER) of MIMO-CR downlink

**Experiment 2:** BER simulation of the proposed uplink MIMO-CR system with LDPC, the simulation parameters are same with Experiment 1. The obtained BER results for PU and SUs are shown in Fig. 8.

Observing simulation results in Fig.8, we find that the PU MS has best BER performance, which in fact is determined by the channel matrix **H**. When SNR is larger than 9dB, the BER of PU is smaller than  $10^{-5}$ , while BER of SU2 is smaller than  $10^{-5}$ , SNR needs to be larger than 15dB. The problem comes the second term of (6), where  $\mathbf{H}^{-1}$  may enlarge the  $\left\lceil n_{1}^{(k)} \right\rceil$ 



Fig.8 The bit error rates (BER) of MIMO CR uplink

# 5. Conclusions

In this paper, we proposed a CSM system with inversed channel matrices precoding and decoding algorithms for MIMO-CR network to enable MSs of PUs and SUs sharing a common channel. The CSM framework and algorithms of downlink and uplink are provided. It is possible to make PUs and SUs work at independent spatial channels in the MIMO-CR downlink and uplink. The simulation results showed that the proposed MIMO-CR network can achieve the good error rate performance in Rayleigh channels. Because MS has no complicated matrix decoding and channel estimation, the implementation of MSs becomes easy and can be accepted in future MIMO-CR network.

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