# A Novel SVPWM Modulation Algorithm of Voltage Source Rectifier with Minimized Switching Losses 

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#### Abstract

Since PWM voltage source rectifier (VSR) can not only provide high-quality DC voltage but also realize four-quadrant operation, it is widely used in many applications. In order to improve the overall efficiency of rectifier, it is required to reduce its switching count and switching loss. Given that the switching loss of rectifier is closely related with its modulation algorithms, the existing modulation algorithms should be optimized. At first, what presented in the paper is the theoretical derivation of the multi-solution principle of VSR, as well as the theoretical analysis of the essential relationship between SPWM and SVPWM. Then the minimized switching loss SPWM and SVPWM modulation algorithms injecting zero-sequence component into the objective function of rectifier are presented, and a power loss formula of power device is also provided. The rectifier with minimized switching loss SPWM and SVPWM modulation algorithms is simulated by means of MATLAB/SIMULINK. Then the experimental platform of VSR with minimized switching loss PWM modulation algorithm is realized based on DSP F28335, which has verified the above theoretical analysis and simulation results. The results show that the overall efficiency of the rectifier with minimized switching loss PWM modulation algorithm increases about $2 \sim 3 \%$ compared to traditional SPWM and SVPWM modulation algorithms.


Key words: - Voltage source rectifier; Multi-solution; Objective function; Zero-sequence component; Minimized switching loss PWM

## 1 Introduction

With the development of the related technologies, three-phase voltage source rectifier (VSR) is now widely used in varies kinds of applications. Since VSR can not only provide high-quality DC voltage but also realize adjustable input power factor and four-quadrant operation, it has significant social and economic benefits[1-3].

For high power rectifier, higher power causes more switching loss to power devices, which results in harder heat dissipation handling, higher heat dissipation cost and lower power conversion efficiency.

In order to reduce the switching loss of VSR, the paper begins to study from its power circuits and modulation algorithms. A three-phase PWM rectifier in Ref. 5, which employs bidirectional switches and minimized switching loss modulation algorithm, is able to greatly increase its overall efficiency[4]. However, as regards the conventional three-phase bridge PWM VSR, it's the only way to reduce
switching loss that a novel PWM modulation algorithm is proposed.

Since PWM rectifier is actually a PWM inverter operating in a different condition, we can maintain power switch stable over a period of time by injecting zero-sequence component into the objective function of rectifier to decrease the equivalent switching frequency and, therefore, reduce switching loss.

Based on the multiple-solution principle of VSR, a novel SPWM modulation algorithm that injects proper zero-sequence component into the objective function of rectifier is presented to minimize switching loss. And it is actually implemented by using the same zero-vector every $60^{\circ}$ in space vector region. Moreover, the minimized switching loss VSR is simulated by means of MATLAB/SIMULINK and the above results are verified by experiments.

## 2 General Solution of VSR

As illustrated in Figure 1, the three-phase VSR is a kind of boost AC-DC converter, which consists of
three-phase AC voltage sources, three-phase boost inductors, 3H-bridge power device arrays and DC energy storage and filter part. In the three-phase VSR, 3H-bridge power device arrays are composed of six reverse inducting switches which include S 1 and D 1 , S3 and D3, S5 and D5, S4 and D4, S6 and D6, S2 and D 2 , that is each reverse inducting switch consists of an IGBT and an anti-paralleled freewheeling diode (FWD).


Figure 1. Power circuit of three-phase VSR
To facilitate the study, we assume that three-phase input voltages are symmetric and balanced with no negative-sequence component or zero-sequence component and three-phase input currents are continuous.

Defining $\mathrm{k}=\mathrm{a}, \mathrm{b}, \mathrm{c}$, which represent three phases. Two-valued logic switching function $S_{\mathrm{k}}$ is given as:

$$
S_{\mathrm{k}}= \begin{cases}1, & \text { uppersideswitchon lower: }  \tag{1}\\ 0, & \text { uppersideswitchoff lower }\end{cases}
$$

Considering the symmetry of three-phase system, three-phase input voltages and currents are given as:

$$
\begin{align*}
& e_{\mathrm{a}}+e_{\mathrm{b}}+e_{\mathrm{c}} \#  \tag{2}\\
& i_{\mathrm{a}}+i_{\mathrm{b}}+i_{\mathrm{c}} \neq \tag{3}
\end{align*}
$$

With the Kirchhoff voltage law and Kirchhoff current law, the equation of voltage-loop at AC side and the nodal equation of current at DC side are obtained as:

$$
\begin{gather*}
L_{1} \frac{\mathrm{~d} i_{\mathrm{k}}}{\mathrm{dt}}=e_{\mathrm{k}}-R_{1} i_{\mathrm{k}}-U_{\mathrm{dc}}\left(S_{\mathrm{k}}-\frac{1}{3} \sum_{\mathrm{k}=\mathrm{a}, \mathrm{~b}, \mathrm{c}} S_{\mathrm{k}}\right)  \tag{4}\\
C_{1} \frac{\mathrm{~d} U_{\mathrm{dc}}}{\mathrm{dt}}=i_{\mathrm{a}} S_{\mathrm{a}}+i_{\mathrm{b}} S_{\mathrm{b}}+i_{\mathrm{c}} S_{\mathrm{c}}-\frac{U_{\mathrm{dc}}}{R_{\mathrm{L}}} \tag{5}
\end{gather*}
$$

Introducing FFT to switching function, Sk can be derived as:

$$
\begin{equation*}
S_{\mathrm{k}}=d_{\mathrm{k}}+\sum_{n=1}^{\infty}(-1)^{n} \frac{2}{n \pi} \sin \left(n d_{\mathrm{k}} \pi\right) \cos \left(n \omega_{\mathrm{s}} t\right) \tag{6}
\end{equation*}
$$

Where, $d_{\mathrm{k}}$ is the average value of switching function $S_{\mathrm{k}}$ in one carrier cycle, or PWM duty cycle. Substituting equation 4 and equation 5 into equation 6 and ignoring the high-frequency components of FFT
spectrum for convenience, the low-frequency mathematical model of three-phase VSR based on duty cycle is obtained as[5,6]:

$$
\begin{gather*}
L_{1} \frac{\mathrm{~d} i_{\mathrm{k}}}{\mathrm{dt}}=e_{\mathrm{k}}-R_{1} i_{\mathrm{k}}-U_{\mathrm{dc}}\left(d_{\mathrm{k}}-\frac{1}{3} \sum_{\mathrm{k}=\mathrm{a}, \mathrm{~b}, \mathrm{c}} d_{\mathrm{k}}\right)  \tag{7}\\
C_{1} \frac{\mathrm{~d} U_{\mathrm{dc}}}{\mathrm{dt}}=i_{\mathrm{a}} d_{\mathrm{a}}+i_{\mathrm{b}} d_{\mathrm{b}}+i_{\mathrm{c}} d_{\mathrm{c}}-\frac{U_{\mathrm{dc}}}{R_{\mathrm{L}}} \tag{8}
\end{gather*}
$$

When selecting duty cycle $d_{\mathrm{k}}$ as the variable, the low-frequency mathematical model of three-phase VSR can be modified as:

$$
\begin{equation*}
\mathbf{A X}=\mathbf{B} \tag{9}
\end{equation*}
$$

Where:

$$
\begin{gather*}
\mathbf{X}=\left[d_{\mathrm{a}}, d_{\mathrm{b}}, d_{\mathrm{c}}\right]^{\mathrm{T}}  \tag{10}\\
\mathbf{A}=\left[\begin{array}{ccc}
2 / 3 & -1 / 3 & -1 / 3 \\
-1 / 3 & 2 / 3 & -1 / 3 \\
-1 / 3 & -1 / 3 & 2 / 3 \\
i_{\mathrm{a}} & i_{\mathrm{b}} & i_{\mathrm{c}}
\end{array}\right]  \tag{11}\\
\mathbf{B}=\left[\begin{array}{l}
\left(e_{\mathrm{a}}-R_{\mathrm{l}} i_{\mathrm{a}}-L_{1} \frac{\mathrm{~d} i_{\mathrm{a}}}{\mathrm{dt}}\right) / U_{\mathrm{dc}} \\
\left(e_{\mathrm{b}}-R i_{\mathrm{b}}-L_{1} \frac{\mathrm{~d} i_{\mathrm{b}}}{\mathrm{dt}}\right) / U_{\mathrm{dc}} \\
\left(e_{\mathrm{c}}-R i_{\mathrm{c}}-L_{1} \frac{\mathrm{~d} i_{\mathrm{c}}}{\mathrm{dt}}\right) / U_{\mathrm{dc}} \\
C_{1} \frac{\mathrm{~d} U_{\mathrm{dc}}}{\mathrm{dt}}+\frac{U_{\mathrm{dc}}}{R_{\mathrm{L}}}
\end{array}\right] \tag{12}
\end{gather*}
$$

With equation 2 and 3, the solution of equation 9 is obtained as:

$$
\mathbf{X}=\left[\begin{array}{l}
\left(e_{\mathrm{a}}-R_{1} i_{\mathrm{a}}-L_{1} \frac{\mathrm{~d} i_{\mathrm{a}}}{\mathrm{dt}}\right) / U_{\mathrm{dc}}  \tag{13}\\
\left(e_{\mathrm{b}}-R_{\mathrm{l}} i_{\mathrm{b}}-L_{1} \frac{\mathrm{~d} i_{\mathrm{b}}}{\mathrm{dt}}\right) / U_{\mathrm{dc}} \\
\left(e_{c}-R_{1} i_{c}-L_{1} \frac{\mathrm{~d} i_{c}}{\mathrm{dt}}\right) / U_{\mathrm{dc}}
\end{array}\right]+\left[\begin{array}{l}
u_{0} \\
u_{0} \\
u_{0}
\end{array}\right]
$$

Where, $u_{\mathrm{k}}=e_{\mathrm{k}}-R_{1} i_{\mathrm{k}}-L_{1} \frac{\mathrm{~d} i_{\mathrm{k}}}{\mathrm{dt}}$ represents the neutral-point voltage function of each bridge, $\left(e_{\mathrm{k}}-R_{1} i_{\mathrm{k}}-L_{1} \frac{\mathrm{~d} i_{\mathrm{k}}}{\mathrm{dt}}\right) / U_{\mathrm{dc}}$ represents the duty cycle function of the neutral-point of each bridge, $u_{0}$ is any zero-sequence voltage component added. The neutral-point voltage modulation of each bridge is defined as:

$$
\begin{equation*}
m=U_{\mathrm{km}} / U_{\mathrm{dc}} \tag{14}
\end{equation*}
$$

Where, $U_{\mathrm{km}}$ is the magnitude of the neutral-point voltage of each bridge.

As shown in Figure 1, point O and $\mathrm{O}^{\prime}$ are connected together to facilitate the study. The initial phase of grid voltage is set as $\theta_{\mathrm{m}}$, the initial phase of the inductor current is set as $\theta_{\mathrm{L}}$, the initial phase of the neutral-point objective voltage $u_{\mathrm{a}}$ of a-phase bridge relative to the voltage of grid side is set as $\theta_{\mathrm{B}}$. Thus, equation 13 is modified as:

$$
\begin{align*}
\mathbf{X} & =\left[\begin{array}{l}
m \sin \left(\omega t+\theta_{\mathrm{B}}\right) \\
m \sin \left(\omega t+\theta_{\mathrm{B}}-2 \pi / 3\right) \\
m \sin \left(\omega t+\theta_{\mathrm{B}}+2 \pi / 3\right)
\end{array}\right]+\left[\begin{array}{l}
d_{0} \\
d_{0} \\
d_{0}
\end{array}\right]  \tag{15}\\
& =\left[\begin{array}{l}
d_{\mathrm{ap}} \\
d_{\mathrm{bp}} \\
d_{\mathrm{cp}}
\end{array}\right]+\left[\begin{array}{l}
d_{0} \\
d_{0} \\
d_{0}
\end{array}\right]
\end{align*}
$$

Where, $m \in[0,1]$ is the modulation, $d_{\mathrm{kp}}$ is the positive-sequence component of switching function $d_{\mathrm{k}}$, while $d_{0}$ is its zero-sequence component. Due to the switching function $d_{\mathrm{k}} \in[0,1]$, the value range of zero-sequence $d_{0}$ should meet the following condition:

$$
\begin{equation*}
0 \leq d_{\mathrm{kp}}+d_{0} \leq 1 \tag{16}
\end{equation*}
$$

Based on the above said, the solution of switching function of the rectifier with symmetric and balanced three-phase input voltages and currents has the following characteristics: (1) there is only one positive-sequence component in steady state whose magnitude is exactly the voltage modulation m ; (2) there are varies zero-sequence components satisfying equation 16.

By injecting different zero-sequence components into objective function, different kinds of PWM modulation algorithms can be obtained, such as SPWM, SVPWM and minimized switching loss PWM[7-9].

## 3 The Principle of Minimized Switching Loss Modulation Algorithm

### 3.1 Traditional SPWM Modulation Algorithm

All the existing modulation algorithms of VSR satisfy the general expression of switching function. Based on high-frequency synthesis theory[10-11] and the operation progress of VSR, the general expression of switching function of the rectifier with bipolar modulation algorithm is given as:

$$
\left\{\begin{array}{l}
m_{\mathrm{H}}(t)=\frac{1}{2}\left(1+\frac{g(t)}{U_{\mathrm{dc}} / 2}\right)  \tag{17}\\
m_{\mathrm{H}}(t)=\frac{1}{2}\left(1-\frac{g(t)}{U_{\mathrm{dc}} / 2}\right)
\end{array}\right.
$$

Where, $\quad m_{\mathrm{H}}(t)$ and $m_{\mathrm{L}}(t)$ are the switching functions of upper side switch and lower side switch on a bridge of VSR, respectively. They meet the conditions: $0 \leq m_{\mathrm{H}}(t) \leq 1,0 \leq m_{\mathrm{L}}(t) \leq 1$, and $m_{\mathrm{H}}(t)+m_{\mathrm{L}}(t)=1 。 g(t)$ is the expected output voltage objective function of VSR, $U_{d c}$ is the DC voltage of VSR that may contains ripple voltages. Under linear modulation, the magnitude of $g(t)$ is below $U_{\mathrm{dc}} / 2$, and the ratio of $g(t)$ to $U_{\mathrm{dc}} / 2$ is exactly the modulation (maximum linear modulation is 1 ).
$g(t)$ is the fundamental component of the neutral-point voltage of each bridge of VSR, as can be any waveform satisfying the requirements. Since three objective functions of the three bridges have $120^{\circ}$ phase differences and the power switches work independently, there can be varies kinds of switch combinations representing zero-vector and nonzero-vector in each switching cycle[12].

### 3.2 Traditional SVPWM Modulation Algorithm

The three input phase voltages and line voltages are given as:

$$
\begin{align*}
& \left\{\begin{array}{l}
u_{\mathrm{a}}=U_{\mathrm{m}} \sin \left(\omega_{i} t\right) \\
u_{\mathrm{b}}=U_{\mathrm{m}} \sin \left(\omega_{i} t-2 \pi / 3\right) \\
u_{\mathrm{c}}=U_{\mathrm{m}} \sin \left(\omega_{i} t+2 \pi / 3\right)
\end{array}\right.  \tag{18}\\
& \left\{\begin{array}{l}
u_{\mathrm{ab}}=\sqrt{3} U_{\mathrm{m}} \sin \left(\omega_{i} t+\pi / 6\right) \\
u_{\mathrm{bc}}=\sqrt{3} U_{\mathrm{m}} \sin \left(\omega_{i} t+\pi / 6-2 \pi / 3\right) \\
u_{c a}=\sqrt{3} U_{\mathrm{m}} \sin \left(\omega_{i} t+\pi / 6+2 \pi / 3\right)
\end{array}\right. \tag{19}
\end{align*}
$$

Where, $U_{\mathrm{m}}$ is the magnitude of phase voltage; $\omega_{\mathrm{i}}$ is the rotational frequency of grid voltage.

In traditional SVPWM, the eight switch combinations are all used to produce different neutral-point voltages, which can be transformed to eight space vectors with fixed location through PARK transformation, as depicted in Figure 2. In the figure, the length of nonzero-vector is $(2 / \sqrt{3}) U_{\mathrm{dc}}$, and switch combination " XXX " is the two-valued function of three bridges, where " 1 " indicates upper side switch on and lower side switch off, " 0 " indicates upper side switch off and lower side switch on.


Figure 2. The distribution of voltage space vectors
When entering different section, the reference voltage space vector $U_{\text {ref }}$ is synthesized by two nonzero-vector and two zero-vector surrounding the section. The duty cycles of nonzero-vector and zero-vector are determined as:

$$
\begin{align*}
& \left\{\begin{array}{l}
d_{\alpha}=\left(\sqrt{3} U_{\mathrm{m}} / U_{\mathrm{dc}}\right) \sin \left(\pi / 3-\omega_{\mathrm{i}} t\right) \\
d_{\beta}=\left(\sqrt{3} U_{\mathrm{m}} / U_{\mathrm{dc}}\right) \sin \left(\omega_{\mathrm{i}} t\right) \\
d_{0}=1-\left(d_{\alpha}+d_{\beta}\right)
\end{array}\right.  \tag{20}\\
& \left\{\begin{array}{l}
d_{7}=k \cdot d_{0} \\
d_{8}=(1-k) \cdot d_{0}
\end{array}\right. \tag{21}
\end{align*}
$$

Where, $d_{\alpha}$ is the duty cycle function of vector $\alpha$ of the section where the reference vector is located, $d_{\alpha} \in[0,1] ; \quad d_{\beta}$ is the duty cycle function of vector $\beta$ of the section where the reference vector is located, $d_{\beta} \in[0,1] ; d_{0}$ is the total duty cycle function of zero-vector, $d_{0} \in[0,1], d_{\alpha}+d_{\beta}+d_{0}=1 ; d_{7}$ is the duty cycle function of the zero-vector with three upper side switches on, while $d_{8}$ is the duty cycle function of the zero-vector with three upper side switches off; k is constant, $k \in[0,1]$.

Taking section 2 for an example, the switching mode for traditional 8 -segment SVPWM using zero-vector $\mathrm{U}_{7}$ in the middle of switching cycle is shown in Figure 3.


Figure 3. The switching mode of traditional 8-segment SVPWM in section 2.

### 3.3 Minimized Switching Loss SPWM Modulation Algorithm

With equation 15 , when adopting traditional SPWM modulation algorithm, the input sinusoidal objective functions of a-phase, b-phase and c-phase are given as:

$$
\left\{\begin{array}{l}
u_{\text {aref }}=m \sin \left(\omega_{i} t+\theta_{B}\right)  \tag{22}\\
u_{\text {bref }}=m \sin \left(\omega_{i} t+\theta_{B}-2 \pi / 3\right) \\
u_{\text {cref }}=m \sin \left(\omega_{i} t+\theta_{B}+2 \pi / 3\right)
\end{array}\right.
$$

According to SPWM modulation algorithm, we select a zero-sequence component as:

$$
\begin{align*}
u_{0} & =-\mathrm{k} \cdot \max \left(u_{\text {aref }}, u_{\text {bref }}, u_{\text {cref }}\right) \\
& -(1-\mathrm{k}) \cdot \min \left(u_{\text {aref }}, u_{\text {bref }}, u_{\text {cref }}\right)  \tag{23}\\
& +(2 \mathrm{k}-1)
\end{align*}
$$

Thus, the new non-sinusoidal objective functions of a-phase, b-phase and c-phase are given as:

As seen in equation 24, different zero-voltage vectors lead to different objective function waveforms. When the modulation changed, the objective function will change accordingly, and $u_{0}$ will change too.

The three-phase VSR with minimized switching loss SPWM modulation algorithm is simulated by MATLAB/SIMULINK. The simulation conditions are as follows: grid voltage is the standard commercial power; the expected value of output DC voltage is 650 V ; the value of load resistor is $50 \Omega$ and the output power is 8.45 kW . Thus, in unity power factor, the RMS value of phase current is calculated as 12.805 A and the magnitude of phase current is calculated as 18.106 A .

Assuming the initial phase of grid voltage is $\theta_{\mathrm{m}}=0$ and the rectifier is working in the state of inductive reactive power, where inductor current lags grid voltage $15^{\circ}$. In this state, the reactive component of inductor current is calculated as $I_{q}^{*}=\sqrt{\frac{3}{2}} \cdot \operatorname{tg}\left(-15^{\circ}\right) \cdot 18.106=-5.942 \mathrm{~A} \quad$ and $\quad$ the active component of inductor current is calculated as $I_{d}^{*}=\sqrt{\frac{3}{2}} \cdot 18.106=22.2 \mathrm{~A}$. The simulation values of the two components of inductor current are -5.942A and 22.6 A , respectively. The neutral-point voltage of each
bridge, whose magnitude is 604 V , lags grid voltage $11.20^{\circ}$. The dead time of PWM driving signal is set as 0 .

If $k=0$, the zero-sequence is given as:

$$
\begin{equation*}
u_{0}=-\left[1+\min \left(u_{\text {aref }}, u_{\text {bref }}, u_{\text {cref }}\right)\right] \tag{25}
\end{equation*}
$$

In this case, the lower switch is turned on for $120^{\circ}$ to achieve minimized switching loss SVPWM, and the objective function of a-phase is shown in Figure 4.


Figure 4. The objective function of a-phase with $\mathrm{k}=0$
If $k=0.5$, the zero-sequence is given as:

$$
\begin{align*}
u_{0} & =-\left[\max \left(u_{\text {aref }}, u_{\text {bref }}, u_{\text {cref }}\right)\right. \\
& \left.+\min \left(u_{\text {aref }}, u_{\text {bref }}, u_{\text {cref }}\right)\right] / 2 \tag{26}
\end{align*}
$$

In this case, the objective function of a-phase is shown in Figure 5, which indicates that this method is the traditional SVPWM modulation algorithm.


Figure 5. The objective function of a-phase with $\mathrm{k}=0.5$
If $k=1$, the zero-sequence is given as:

$$
\begin{equation*}
u_{0}=1-\max \left(u_{\text {aref }}, u_{\text {bref }}, u_{\text {bref }}\right) \tag{27}
\end{equation*}
$$

In this case, the upper switch is turned on for $120^{\circ}$ to achieve minimized switching loss SVPWM, and the objective function of a-phase is shown in Figure 6.


Figure 6. The objective function of a-phase with $\mathrm{k}=1$
If $k$ is switched between 0 and 1 every $60^{\circ}$, the zero-sequence is given as:

$$
u_{0}=\left\{\begin{array}{lll}
-\min \left(u_{\text {aref }},\right. & u_{\text {bref }}, & \left.u_{\text {cref }}\right)-1 \tag{28}
\end{array} \quad k=0, ~\left(u_{\text {bref }}, u_{\text {bref }}, u_{\text {cref }}\right)+1 \quad k=1\right.
$$

In this case, the upper switch and lower switch are both turned on for $60^{\circ}$ to achieve minimized switching loss SVPWM, and the objective function of a-phase is shown in Figure 7.


Figure 7. The objective function of a-phase with $k=0 / 1$

### 3.4 Minimized Switching Loss SVPWM Modulation Algorithm

Due to the symmetric control of traditional SVPWM VSR, the power loss of each reverse conducting switch, which consists of IGBT and FWD, is equal. The power loss includes conducting loss and switching loss, as is determined by[13]:

$$
\begin{equation*}
P_{\mathrm{Loss}}=g\left(\bar{U}_{\mathrm{ce}}, \bar{I}_{\mathrm{c}}\right) \bar{f}_{\mathrm{s}} \tag{29}
\end{equation*}
$$

Where, $U_{\mathrm{ce}}$ is the average conduction voltage drop across power switch, $I_{\mathrm{c}}$ is the average conduction current flowing through power switch, $f_{\mathrm{s}}$ is the average switching frequency of power switch, $P_{\text {Loss }}$ is the average power loss of power switch, which is a monotonically increasing function of $U_{\mathrm{ce}}$ and $I_{\mathrm{c}}$, and reversely proportional to $f_{\mathrm{s}}$.

The above power loss calculation expression is also applied to FWD.

For traditional SVPWM modulation algorithm, $\bar{U}_{\mathrm{ce}}, \bar{I}_{\mathrm{c}}$ and $\bar{f}_{\mathrm{s}}$ are not optimized in every section and every switching cycle where $\bar{f}_{\mathrm{s}}$ is equal to carrier frequency $f_{c}$, which results in much switching loss.

As illustrated in Figure 2, any three adjacent vectors share a same bit ( 1 or 0 ), which means that there can be one bridge at most not working to reduce the switching count by one thirds at most. By using the same zero-vector (111 or 000) on both sides of the phase current peak, the minimized switching loss modulation algorithm can not only reduce switching count by one thirds but also avoid switching around the phase current peak(that is $\left(60^{\circ}, 120^{\circ}\right)$ and
$\left(240^{\circ}, 300^{\circ}\right)$ ). Therefore, the maximum peak value of phase current where switch is switching can be reduced by $1-\sqrt{3} / 2$ and the switching loss can be reduced by more than one thirds.

There are two methods to realize minimized switching loss SVPWM modulation algorithm, which include single zero-vector modulation and double zero-vector modulation.

Single zero-vector modulation uses only one zero-vector in all sections of voltage space vector plane: $U_{7}$ or $U_{8}$, which correspond to $\mathrm{k}=1$ and $\mathrm{k}=0$ in equation 21, respectively. Even though this modulation algorithm can reduce switching loss dramatically, it introduces lots of harmful harmonic voltages. The two methods of single zero-vector modulation are named method one and method two, respectively.

While, double zero-vector modulation uses zero-vector $U_{7}$ ( $\mathrm{k}=1$ ) in section I, III, V and $U_{8}$ $(\mathrm{k}=0)$ in section II, IV, VI, as is named method three. It can also uses zero-vector $U_{8} \quad(\mathrm{k}=0)$ in section I, III, V and $U_{7}$ ( $\mathrm{k}=1$ ) in section II, IV, VI, as is named method four.

As for method one and method two, there can be a period of $120^{\circ}$ in every output cycle when two power switches of each bridge are not chopping and cause no switching loss. However, one disadvantage of the two methods is that their control is not symmetric, which brings about non-uniform heat to two power switches of each bridge.

As for method three and method four, there can be a period of $60^{\circ}$ in both positive half and negative half of output cycle with an interval of $180^{\circ}$ when two power switches of each bridge are not chopping and cause no switching loss. Moreover, they will cause no asymmetric control problem and bring uniform heat to two power switches of each bridge[14,15].

The above four methods can all reduce the average switching frequency by one thirds relative to carrier frequency. According to equation 29, the switching loss is related with the angle between the expected input voltage and current $\left(\theta_{\mathrm{L}}-\theta_{B}\right)$, which is also a monotonically increasing function of $U_{\mathrm{ce}}$ and $I_{c}$.

In order to reduce switching loss further, the fifth method of double zero-vector modulation algorithm is proposed. The method five places the switching point of the value of $k$ at the centre line of each section to realize that the $60^{\circ}$ non-switching sections in both positive half and negative half of output cycle are placed on both sides of the phase current peak
symmetrically, as shown in Figure 8. In the $30^{\circ}$ regions on each side of the phase current peak of positive half of output cycle, the upper side switch is on, while the lower one is off. On the contrary, in the $30^{\circ}$ regions on each side of the phase current peak of negative half of output cycle, the upper side switch is off, while the lower one is on. In this way, the switching loss can be dramatically reduced, especially for high frequency and high phase current applications.

Defining the angle by which the $60^{\circ}$ non-switching section's central line lags grid voltage peak point as the non-switching section's lag angle $\delta$. If $\delta$ is equal to $\theta_{\mathrm{m}}-\theta_{\mathrm{L}}$, two $60^{\circ}$ non-switching sections will be located in the two $60^{\circ}$ sections around the phase current peak in both positive and negative half of output cycle. Based on


Figure 8. Minimized switching loss SVPWM modulation algorithm
inductive reactive power or capacitive reactive power delivered to the grid by rectifier, $\theta_{\mathrm{m}}-\theta_{\mathrm{L}}$ is set as positive value and negative value, respectively. Defining $\delta^{\prime}=\delta-30^{\circ}$ to facilitating the analysis, so $\delta, \delta^{\prime}, \theta_{\mathrm{m}}-\theta_{\mathrm{L}}$ and k are given as:

$$
\begin{align*}
& \delta= \begin{cases}\theta_{\mathrm{m}}-\theta_{\mathrm{L}} & \left|\theta_{\mathrm{m}}-\theta_{\mathrm{L}}\right| \leq 30^{\circ} \\
30^{\circ} & \theta_{\mathrm{m}}-\theta_{\mathrm{L}}>30^{\circ} \\
-30^{\circ} & \theta_{\mathrm{m}}-\theta_{\mathrm{L}}<-30^{\circ}\end{cases}  \tag{30}\\
& \mathrm{k}= \begin{cases}1 & \omega_{0} t \in\left[330^{\circ}+\delta^{\prime}, 360^{\circ}\right] \\
& \mathrm{U}\left[0,30^{\circ}+\delta^{\prime}\right] \\
0 & \omega_{\mathrm{o}} t \in\left[30^{\circ}+\delta^{\prime}, 90^{\circ}+\delta^{\prime}\right] \\
1 & \omega_{\mathrm{o}} t \in\left[90^{\circ}+\delta^{\prime}, 150^{\circ}+\delta^{\prime}\right] \\
0 & \omega_{\mathrm{o}} t \in\left[150^{\circ}+\delta^{\prime}, 210^{\circ}+\delta^{\prime}\right] \\
1 & \omega_{\mathrm{o}} t \in\left[210^{\circ}+\delta^{\prime}, 270^{\circ}+\delta^{\prime}\right] \\
0 & \omega_{0} t \in\left[270^{\circ}+\delta^{\prime}, 330^{\circ}+\delta^{\prime}\right]\end{cases} \tag{31}
\end{align*}
$$

Where, $\omega_{0}$ is the rotational frequency of grid voltage.

$$
\text { If }\left|\theta_{\mathrm{m}}-\theta_{\mathrm{L}}\right| \leq 30^{\circ} \text { and } \cos \left(\theta_{\mathrm{m}}-\theta_{\mathrm{L}}\right) \geq 0.866, \text { two } 60^{\circ}
$$ non-switching sections will be located in the two $60^{\circ}$ sections around the phase current peak in both positive and negative half of output cycle. Due to the four-quadrant operation of VSR, equation 31 is very useful. For example, when the rectifier is working with unity power factor ( $\left.\delta=\theta_{\mathrm{m}}-\theta_{\mathrm{L}}=0\right)$, the zero-vector varying with $\omega_{0} t$ is given as:

$$
U_{\mathrm{o}}= \begin{cases}111 & \omega_{\mathrm{o}} t \in\left[0^{\circ}, 30^{\circ}\right]  \tag{32}\\ 000 & \omega_{\mathrm{o}} t \in\left[30^{\circ}, 90^{\circ}\right] \\ 111 & \omega_{\mathrm{o}} t \in\left[90^{\circ}, 150^{\circ}\right] \\ 000 & \omega_{0} t \in\left[150^{\circ}, 210^{\circ}\right] \\ 111 & \omega_{\mathrm{o}} t \in\left[210^{\circ}, 270^{\circ}\right] \\ 000 & \omega_{\mathrm{o}} t \in\left[270^{\circ}, 330^{\circ}\right] \\ 111 & \omega_{\mathrm{o}} t \in\left[330^{\circ}, 360^{\circ}\right]\end{cases}
$$

The three-phase VSR with minimized switching loss SVPWM modulation algorithm is simulated by MATLAB/SIMULINK. The simulation conditions are as follows: grid voltage is the standard commercial power; selecting $680 \mu \mathrm{~F}$ electrolytic capacitor and 10 mH inductor with ESR of $0.1 \Omega$; the expected average voltage of DC loop is set as 650 V ; The rectifier is operating in power supply state with resistive loads, whose output power is 8.45 kW ; Switching frequency is 10 khz ; Dead time is not considered in the simulation.

In unity input power factor state, Figure 9 shows (a) the voltage across the upper switch S 1 , (b) the current flowing through S1 and the input current of a-phase, (c) the current flowing through D 4 , (d) the switching function of a-phase, (e) the zero-sequence component. The angle between grid voltage and input current is 0 and the angle between the expected input voltage and grid voltage is $\theta_{B}=-10.3^{\circ}$ and the magnitude of neutral-point voltage of a-phase bridge is 620 V .

(a) The voltage across upper side IGBT


1-the current of upper side IGBT S1; 2-input current
(b) The current of upper side IGBT S1 and input current

(c) The current of FRD D4

(d) Synthesized switching function of a-phase

(e) Zero-sequence component

Figure 9. The voltage across switch and current for minimized switching loss modulation algorithm

In capacitive input power factor state, Figure 10 shows (a) the voltage across the upper switch S1, (b) the current flowing through S1 and the input current of a-phase, (c) the current flowing through D4, (d) the switching function of a-phase, (e) the zero-sequence component. The angle between grid voltage and input current is $+15^{\circ}$ and the angle between the expected input voltage and grid voltage is $\theta_{B}=-10.3^{\circ}$ and the magnitude of neutral-point voltage of a-phase bridge is 650 V .

(a) The voltage across upper side IGBT


1-the current of upper side IGBT S1; 2-input current
(b) The current of upper side IGBT S1 and input current


(e) Zero-sequence component

Figure 10. The voltage across switch and current for minimized switching loss modulation algorithm

In inductive input power factor state, Figure 11 shows (a) the voltage across the upper switch S 1 , (b) the current flowing through S1 and the input current of a-phase, (c) the current flowing through D4, (d) the switching function of a-phase, (e) the zero-sequence component. The angle between grid voltage and input current is $-15^{\circ}$ and the angle between the expected input voltage and grid voltage is $\theta_{B}=-10.3^{\circ}$ and the magnitude of neutral-point voltage of a-phase bridge is 604 V .

(a) The voltage across upper side IGBT


1-the current of upper side IGBT S1; 2-input current
(b) The current of upper side IGBT S1 and input current

(c) The current of FRD D4

(d) Synthesized switching function of a-phase

(e) Zero sequence-component

Figure 11. The voltage across switch and current for minimized switching loss modulation algorithm

As seen in the above figures, the minimized switching loss SVPWM modulation algorithm is corrected.

By analyzing the direct power control (DPC) algorithm of PWM VSR, the DPC algorithm is actually similar to minimized switching loss SVPWM algorithm, except for starting point of control and switching frequency[16]. Though combining control with modulation, the switching frequency of DPC algorithm is not fixed, as is bad for inductor selecting and device safe. It is sure that DPC can be modified as direct power SVPWM modulation algorithm with fixed switching frequency. The switching table for DPC is shown in table 1.

Table I. The switching table for DPC

| $S_{\mathrm{p}}$ | $S_{\mathrm{q}}$ |  | $S_{\mathrm{a}}$ |  |  |  |  |  | $S_{\mathrm{b}}$ | $S_{\mathrm{c}}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | I | II | III | IV | V | VI |  |  |  |  |
| 0 | 0 | 101 | 100 | 100 | 110 | 110 | 010 |  |  |  |  |
| 0 | 1 | 100 | 110 | 110 | 010 | 010 | 011 |  |  |  |  |
| 1 | 0 | 101 | 111 | 100 | 000 | 110 | 111 |  |  |  |  |
| 1 | 1 | 111 | 111 | 000 | 000 | 111 | 111 |  |  |  |  |
| $S_{\mathrm{p}}$ | $S_{\mathrm{q}}$ | VII | VIII | IX | X | XI | XII |  |  |  |  |
| 0 | 0 | 010 | 011 | 011 | 001 | 001 | 101 |  |  |  |  |
| 0 | 1 | 011 | 001 | 001 | 101 | 101 | 100 |  |  |  |  |
| 1 | 0 | 010 | 000 | 011 | 111 | 001 | 000 |  |  |  |  |
| 1 | 1 | 000 | 000 | 111 | 111 | 000 | 000 |  |  |  |  |

### 3.5 The Loss Calculation for Minimized Switching Loss SVPWM Modulation Algorithm

Defining the angle between inductor current and neutral-point voltage of each bridge as $\theta_{\mathrm{LB}}=\theta_{\mathrm{L}}-\theta_{\mathrm{B}}$. Based on the phase relationship between switching function and input current, the average conducting loss of the power switch (IGBT) and freewheeling diode (FWD) is determined as:

$$
\begin{align*}
& P_{\mathrm{S} 1}=\frac{1}{2 \pi} \int_{0}^{\pi} \frac{1-u_{\mathrm{aref}}}{2} u_{\mathrm{ce}(\mathrm{sat})} \cdot I_{\mathrm{p}} \sin \left(\omega_{\mathrm{i}} t-\theta_{\mathrm{LB}}\right) d \omega_{\mathrm{i}} t  \tag{33}\\
& P_{\mathrm{D} 1}=\frac{1}{2 \pi} \int_{0}^{\pi} \frac{1+u_{\mathrm{aref}}^{\prime}}{2} u_{\mathrm{ce}(\mathrm{sat})} \cdot I_{\mathrm{p}} \sin \left(\omega_{\mathrm{i}} t-\theta_{\mathrm{LB}}\right) d \omega_{\mathrm{i}} t \tag{34}
\end{align*}
$$

Where, $I_{\mathrm{p}}$ is the peak value of input current, $i_{c}=I_{\mathrm{p}} \sin \left(\omega_{\mathrm{i}} t-\theta_{\mathrm{LB}}\right) \cdot u_{\text {ce(sat) }}$ is the saturation voltage drop across power switch, which is a function of collector current ${ }^{i_{\mathrm{c}}}$. Obviously, the conducting loss of IGBT is increasing, while decreasing for FRD compared with traditional SVPWM modulation algorithm.

The average switching loss for IBGT and FWD is determined as:

$$
\begin{gather*}
P_{\mathrm{S} 1}=2 \times 50\left[\int_{0}^{\pi / 6}\left(E_{\text {on }}+E_{\text {off }}\right) d \omega_{\mathrm{i}} t\right.  \tag{35}\\
P_{\mathrm{D} 2}=2 \times 50 \times \int_{0}^{\pi / 6} E_{\text {err }} d \omega_{\mathrm{i}} t \tag{36}
\end{gather*}
$$

Where, $E_{\text {on }}$ and $E_{\text {off }}$ are the power consumption during the turn-on progress and turn-off progress of IGBT respectively, each of which is a function of
collector current $i_{\mathrm{c}} . E_{\text {err }}$ is the power consumption during the reverse recovery progress of FWD, which is a function of forward current $i_{c}$. The switching loss for each IGBT and FWD is greatly reduced compared with traditional SVPWM modulation algorithm.

In the above equations, the voltages across power switch and freewheeling diode vary nonlinearly with the current flowing through them. Refer to the related product specification for calculation.

Taking the IGBT module BSM100GB50DLC of EUPEC for an example, the test conditions are as follows: $\mathrm{V}_{\mathrm{GE}}=15 \mathrm{~V}, \mathrm{R}_{\text {gon }}=\mathrm{R}_{\text {goff }}=18 \Omega$, Uce $=$ $1200 \mathrm{~V}, \mathrm{Tj}=125^{\circ} \mathrm{C}$ 。

The characteristic curves of IGBT and Diode are shown in Figure 12, in which the data provided by firms is the calculation basic for the power loss of power devices.

(a) IGBT output characteristic curve

(b) Diode forward characteristic curve

(c) IGBT and diode reverse recovery power loss curves

Figure 12. IGBT and diode power loss curves
Assuming that the rectifier is operating in power supply state with resistive loads, whose output power is 8.45 kW ; The dead time is set as 0 ; The efficiency of the VSR is $95 \%$; the RMS value of input current is 12.805 A and the magnitude of input current is 18.106A.

By calculation, the conducting loss and switching loss of a-phase's upper switch with minimized switching loss SVPWM modulation algorithm are given as:

Average conducting loss: $\mathrm{P}(\mathrm{S} 1+\mathrm{D} 1) \approx 5.2 \mathrm{~W}$
Average switching loss: $\mathrm{P}(\mathrm{S} 1+\mathrm{D} 1) \approx 52 \mathrm{~W}$
The conducting loss and switching loss of a-phase's upper switch with the traditional SVPWM modulation algorithm are given as:

Average conducting loss $\mathrm{P}(\mathrm{S} 1+\mathrm{D} 1) \approx 3.8 \mathrm{~W}$
Average switching loss: $\mathrm{P}(\mathrm{S} 1+\mathrm{D} 1) \approx 88 \mathrm{~W}$
Therefore, the total loss of a-phase's upper switch is reduced by 34.6 W with minimized switching loss SVPWM modulation algorithm, which means that the total loss of six switches of the rectifier is reduced by 207.6W. Since the output power of the rectifier is 8.45 kW , the efficiency of the rectifier system is improved by $2.4 \%$.

## 4 The Realization Principle of VSR

### 4.1 The Block Diagram of Rectifier System

The three-phase VSR adopts the structure of voltage outer-loop and current inner-loop, where the current inner-loop introduces the minimized switching loss PWM modulation algorithm. The power circuit and control circuit of three-phase VSR with unity power factor at grid side are shown in Figure 13.

The output DC voltage is detected and, then compared with the given output DC voltage to get a voltage error, which can produce the given current of d -axis through PI regulator. Set the given current of q -axis as positive value for capacitive input power factor, while negative value for inductive one. Detect the three-phase grid voltages and input currents with sensor, which can obtain the actual currents of d-axis and $q$-axis through coordinate transformation. In order to achieve the three-phase VSR with unity input power factor, the given current of $q$-axis is set as 0 . The given currents of $d$-axis and $q$-axis minus the actual currents of d -axis and q -axis are the current errors, which can produce the given voltage $U_{d}^{*}$ and $U_{q}^{*}$ through PI regulator, respectively. Then $U_{d}^{*}$ and $U_{q}^{*}$ are transformed to $U_{\alpha}^{*}$ and $U_{\beta}^{*}$ through coordinate transformation, based on which the driving signals can be generated by MCU or DSP to control PIM module.


Figure 13. The power circuit and control circuit of three-phase VSR

### 4.2 Experiment Analysis

In order to verify the above analysis, an experiment is done.

Experiment conditions: standard commercial power with three-phase AC input voltages of 380 VAC and 50 Hz gird frequency; $680 \mu \mathrm{~F}$ electrolytic capacitor, 10 mH inductor; the expected average voltage of DC loop is set as 650 V ; the rectifier is operating in power supply state with resistive loads, whose output power is 8.45 kW ; switching frequency is 10 kHz .

Main components: select 10 mH boost inductor designed by silicon steel whose frequency is 10 kHz and $680 \mu \mathrm{~F}$ filtering capacitor. BSM50GB120DLC: $50 \mathrm{~A} / 80^{\circ} \mathrm{C} / 1200 \mathrm{~V}$ is selected as IGBT driven by TPS2812. DSP TMS320F28335 is chose as the controller, which supports floating point operation.

Experimental purpose: unity power factor at grid side.

By software programming and hardware debugging, the VSR system with minimized switching loss PWM modulation algorithm as shown in Figure 13 is implemented.

In steady state, the measured voltage of DC loop is 650 V , the peak-to-peak value of ripple voltage is 15 V . Figure 14 shows the driving pulse of the lower switch of a-phase after a low pass filter, which is the duty cycle waveform. Figure 15 shows the waveforms of grid voltage and input current with full loads. As seen in the figure, the lower the input current ripple is, the higher the quality of the input current is. Moreover, the input current has the same phase with grid voltage, which means that the input power factor approaches one. By test, within several kW power, the minimized switching loss PWM modulation algorithm can improve the efficiency of
the rectifier system by $2 \sim 3 \%$ over the traditional PWM modulation algorithm, which will be benefit for heat dissipation and system reliability.


Figure 14. Duty cycle of the lower switch of a-phase


Figure 15. The grid voltage and input current with full loads

## 5 Conclusion

Based on the multiple-solution principle of voltage source rectifier and the operation principle of SVPWM and SPWM modulation algorithms, a minimized switching loss PWM modulation algorithm is presented in the paper. The VSR with minimized switching loss SPWM and SVPWM modulation algorithm is simulated and verified by means of MATLAB/SIMULINK, and the power loss calculation of minimized SVPWM is also provided. The above theoretical analysis and simulation results are verified by the experiment based on DSP TMS320F28335 control circuit. The results show that the minimized switching loss PWM modulation algorithm can improve the overall efficiency of the rectifier system by $2 \sim 3 \%$ over the traditional PWM modulation algorithm, which will be benefit for heat dissipation and system reliability.

## References

[1] IEC61000-3-2: 1995 "Electromagnetic compatibility Part3: limits-set.2: limits for harmonic current emission (equipment input current $\leq 16 \mathrm{~A}$ per phase)".
[2] WU Jing-chang. Power system harmonics[M]. Beijing: China electric power press, May 1998.(in chinese)
[3] LIN Hai-xue, SUN Shu-qin. Harmonics in power system[M]. Beijing: China electric power press, April 1998. (in chinese)
[4] YANG Xi-jun, LEI Huai-gang, ZHANG Yong-xin, MA Shao-cai. Research on three-phase partial active power factor correction[J]. Power Electronics, 2010, 44(5): 34-40. (in chinese)
[5] QU Xue-ji, QU Jing-kai, YU Ming-yang. Power electronic rectifier technology and its applications[M]. Beijing: Publishing house of electronics industry, April 2008. (in chinese)
[6] ZHANG Chong-wei, ZHANG Xing. The voltage source rectifier and its control[M]. Beijing: China machine press, October 2003. (in chinese)
[7] XIONG Jian, KANG Yong, ZHANG Kai, CHEN Jian. Comparison study of voltage space vector PWM and conventional SPWM[J]. Power Electronics, 1999, 33(1): 25-28. (in chinese)
[8] Bowes S R, Lai Yenshin. The relationship between space vector modulation and regular-sampled PWM[J]. IEEE Trans on Industrial Electronics. 1997, 44 (5): 670-679.
[9] XIONG Jian. Study on three phase voltage source high frequency PWM rectifier [D]. Wuhan: Huazhong University of Science and Technology, 1999. (in chinese)
[10] M. Venturini and A. Alesina. The generalized transformer: a new bidirectional sinusoidal waveform frequency converter with continuously adjustable input power factor[J]. IEEE PESC' 80 , 1980.
[11] M.G.B. Venturuni, A.Alesina. Solid State Power Conversion: An Analysis Approach to Generalized Transformer Synthesis[J]. IEEE Trans. on Circuit System, CAS-28(4): 319-330, April 1981.
[12] CHEN Hui, LEI Huai-gang, YANG Xi-jun. Voltage space vector PWM interter control method based on switching functions[J]. Electrical automation, 2003, 25(2): 17-19. (in chinese)
[13] Anderson John B. Anderson P M, Herrick R ,et al. Power electronics and variable frequency drives[J]. Piscataway: IEEE Press, 1996.
[14] HUANG Hai, LI Bai-ya, LI Qiang, YIN Jin-tian. Space vector PWM modulating techinique based on minimum swtichi loss[J]. Automation and instrumentation, 2007(1): 5-9. (in chinese)
[15] V. Blasko. Analysis of a hybrid PWM based on modified space-vector and triangle-comparison
methods[J]. IEEE trans. Industry Applications. Vol. 33, pp.756-764, May/June 1997.
[16] WANG Guo-jun, WU Feng-jiang, SUN Li. The comparison between two modulations for PWM
rectifier based on direct power control[J]. Power Electronics, 2008, 42(8): 62-64. (in chinese)

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