

Point of Common Coupling Power Factor Conditioning of Connected Loads with PWM Rectifier

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Abstract: - The proliferation of poor power factor loads can deteriorate the network due to their negative impacts. In this research, a power factor conditioning of PCC is presented as another role of pulse width modulation rectifier. The main purpose of PWM rectifier is to adjust and regulate the output DC-voltage with low harmonic distortion of AC-source current. If inductive loads connected to same PCC, the PWM rectifier can also compensate for load reactive power. These two functions of PWM rectifier can improve overall system power factor and decrease added cost elaborated with equipment required for compensation. The proposed control scheme is based on d-q theory in which transformation from abc to d-q frames is carried out for both load and converter currents. Quadrature portion of load current, which represents load reactive power, will be inserted in current controller with negative phase to compensate for reactive power and improve poor power factor. The proposed control algorithm is realized by a low-cost 80C196KC microcontroller which provides multi-functions adequate for practical system implementation. Inductive load emulation is presented by a three-phase induction motor due to its widespread applications and variable power factor at different mechanical loads.

Key-Words: - PWM rectifier, harmonics, inductive load, power factor, d-q theory, microcontroller

1 Introduction

Power factor exhibits a fundamental index for illustrating power quality and voltage stability in power system. It is well recognized that loads with poor power factor contribute to low voltage quality and increase losses in electric grid. In addition, it reduces grid transmission capacity, substation voltage stability, and can cause voltage breakdown at large load [1- 4]. On the other hand, a relatively little correction in power factor can achieve a significant reduction in system power losses and enhance grid voltage stability and power quality.

Nowadays, active PWM rectifier has a widespread usage in AC/DC conversion according to its different characteristics, such as stabilization of DC-link voltage, bi-directional power flow, harmonic free line current, and displacement factor control [5- 10]. The topology of PWM rectifier, presented in figure 1, shows that it consists of three legs VSI that has its DC-side linked to a smoothing capacitor and AC-side coupled to grid through three-line inductors. This topology enables PWM rectifier to control reactive power alongside its AC/DC conversion. Different control strategies are proposed to operate the PWM rectifier [11-22]. In this paper, a lightly loaded three-phase induction

motor (i.e. poor power factor inductive load) is connected to same PCC of PWM rectifier to test the system performance. The reactive components of motor current (i_q) is extracted by d-q theory and then added with negative sign to current control loop of PWM rectifier.

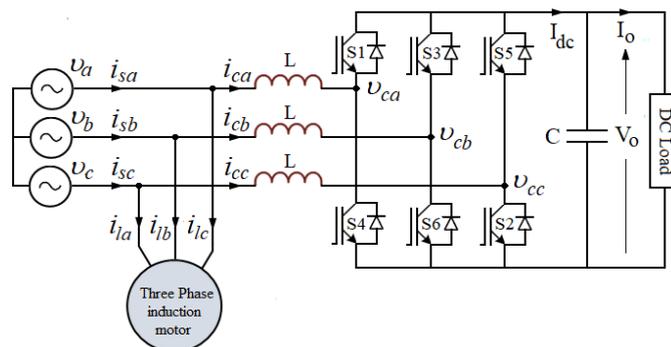


Fig. 1. PWM rectifier and induction motor at same PCC.

In this context, the converter circuit operates as synchronous condenser to generate reactive power demanded by the motor and hence improves overall system power factor.

The switching method of VSI power circuit is functioned by using PWM hysteresis current control scheme. This scheme has the advantages of

straightforwardness in algorithm and perfect spectral performance of line current [23- 27].

2 Theory and Operation

The power circuit of three-phase PWM rectifier in VSI bridge connection is shown in figure 1. In this topology, the DC-link voltage (Vdc) should be controlled as in (1) to emphasize linear PWM operation and steady sinusoidal mains current [28].

$$V_{dc} \geq \frac{2\sqrt{2}}{\sqrt{3}} V_{LL} \quad (1)$$

where; V_{LL} is rms line to line supply voltage.

The circuit shown in figure 2 explains the operation of PWM rectifier, where it represents a single-phase equivalent circuit of PWM rectifier system shown in figure 1. In addition, the phasor diagram of overall system is shown in figure 3. The converter voltage vector (V_{ca}) is used to adjust the phase angle (θ_s) of ac line current (I_{sa}). For unity power factor operation, the magnitude and phase angle of converter voltage is controlled so that θ_s equal zero, and the switching pattern of converter IGBTs emphasizes sinusoidal current waveform. In this manner, the PWM rectifier power circuit delivers the motor reactive power instead of utility mains.

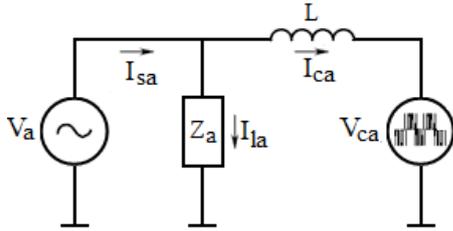


Fig. 2. Single line diagram of the system.

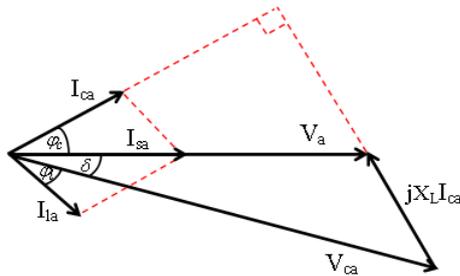


Fig. 3. Phasor diagram of the system.

where; δ is the converter voltage angle, ϕ_c is the converter current angle, and ϕ_1 is the load current angle. Referring to figure 1, equations representing the power circuit are:

$$\begin{bmatrix} i_{sa} \\ i_{sb} \\ i_{sc} \end{bmatrix} = \begin{bmatrix} i_{la} \\ i_{lb} \\ i_{lc} \end{bmatrix} + \begin{bmatrix} i_{ca} \\ i_{cb} \\ i_{cc} \end{bmatrix} \quad (2)$$

$$\begin{bmatrix} L \frac{d}{dt} i_{ca} \\ L \frac{d}{dt} i_{cb} \\ L \frac{d}{dt} i_{cc} \end{bmatrix} = V_{dc} \begin{bmatrix} -\frac{2}{3} & 1 & 1 \\ 1 & -\frac{2}{3} & 1 \\ 1 & 1 & -\frac{2}{3} \end{bmatrix} \begin{bmatrix} S_1 \\ S_3 \\ S_5 \end{bmatrix} + \begin{bmatrix} v_a \\ v_b \\ v_c \end{bmatrix} \quad (3)$$

$$\frac{dV_{dc}}{dt} = \frac{1}{C} (I_{dc} - I_o) \quad (4)$$

$$I_{dc} = S_1 I_{ca} + S_3 I_{cb} + S_5 I_{cc} \quad (5)$$

where S_1, S_3, S_5 are the status (0 or 1) of upper switches.

3 Proposed Control Scheme

There are two main purposes of converter controller; the first one is to eliminate supply current harmonic components, while the second purpose is to adjust and regulate DC output voltage. Additionally, the controller can also compensate for reactive current absorbed by the inductive load. These two functions are accomplished by applying *abc-dq* transformation for both load current and converter current. It is well known that the direct current (i_d) represents the active power, while the quadrature current component (i_q) represents reactive power. By eliminating harmonic and reactive power components from line current, it appears sinusoidal and has almost zero displacement angle. Thus, overall system acts as resistive load and enhance grid power quality.

According to three-phase three-wire system topology, the zero-sequence current is eliminated and *d-q* transformation may be expressed as;

$$K = \frac{2}{3} \begin{bmatrix} \cos(\theta) & \cos(\theta - \frac{2}{3}) & \cos(\theta + \frac{2}{3}) \\ -\sin(\theta) & -\sin(\theta - \frac{2}{3}) & -\sin(\theta + \frac{2}{3}) \end{bmatrix} \quad (6)$$

where; K is the coefficient of transformation, and θ is the instantaneous angle of an arbitrary frequency.

Direct and quadrature components of load current ($i_{l,dq}$) and converter current ($i_{c,dq}$) can be obtained by applying the transformation of equation (6) according to;

$$i_{l,dq} = K i_{l,abc} \quad (7)$$

$$i_{c,dq} = K i_{c,abc} \quad (8)$$

Both direct and quadrature components of converter current ($i_{c,d}, i_{c,q}$) contain DC and AC components as;

$$i_{c,d} = \bar{i}_{c,d} + \tilde{i}_{c,d} \quad (9)$$

$$i_{c,q} = \bar{i}_{c,q} + \tilde{i}_{c,q} \quad (10)$$

Figure 4 presents the block diagram of proposed control system. In this controller, the DC output

voltage is regulated by PI controller, while the reference signal of direct converter current ($i_{c_d}^*$) is generated by adding the DC components of direct converter current ($i_{c_d}^-$) to PI controller output. In addition, to compensate for load reactive power, the negative value of quadrature components of load current ($-i_{l_q}$) is considered the reference quadrature components of converter current ($i_{c_q}^*$).

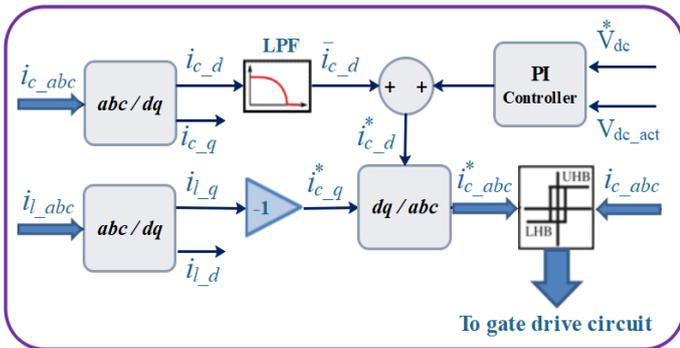


Fig. 4. Blok diagram of proposed control strategy.

4 Simulation Results

A MATLAB/Simulink is used to build the proposed simulation platform to evaluate system performance under different operating conditions as shown in figure 5.

According to equation (1), the DC output voltage is designed to be 700V for better PWM switching performance. A lightly loaded three phase induction motor with a low PF of 0.66 is shunted to PCC. Table I exhibits overall system parameters.

Table 1. System Parameters

Parameter	Value
Line voltage	$V_{LL}=380V$
DC output voltage	$V_{dc-ref}=700V$
filter inductor	$L=5mH$
PWM rectifier load	$R_{load}=50\Omega$
Filter capacitor	$C=1000\mu F$
Induction motor	10 hp, 380V, 50Hz, 90% efficiency, and 0.66 PF at light load.

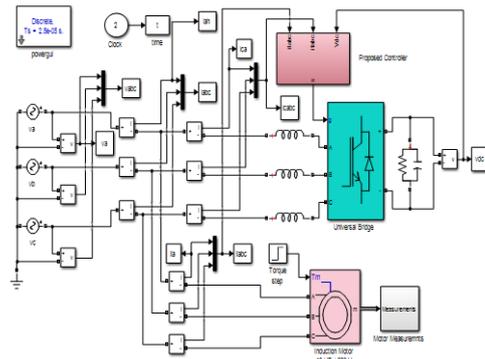


Fig. 5. MATLAB/Simulink model of proposed PWM rectifier system.

Figure. 6 presents the motor line current (i_{la}) at steady state with respect to the source voltage (v_{sa}) and its associated active (P_l) and reactive (Q_l) powers.

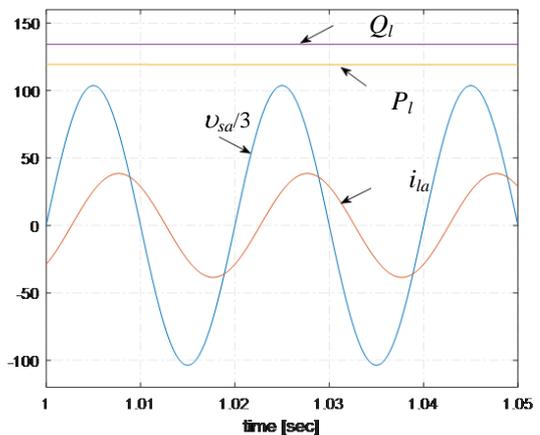


Fig. 6. Induction motor current and its associated powers.

The performance of PWM rectifier system is shown in figure 7 according to proposed controller. The figure exhibits that the source current i_{sa} is almost sinusoidal and with the same phase of source voltage v_{sa} . In addition, the output voltage V_{DC} is adjusted to its predefined value of 700V.

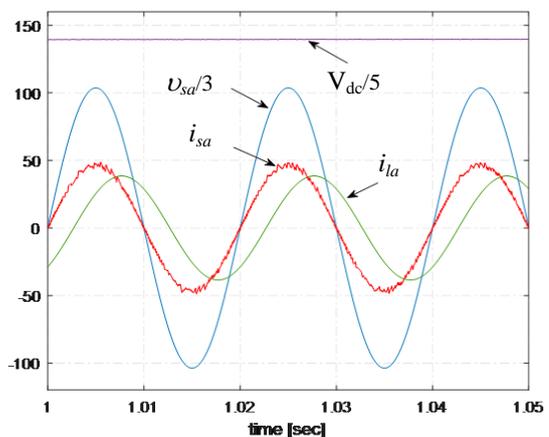


Fig. 7. Performance of PWM rectifier system.

The spectrum of line current is shown in figure 8 as percent of its fundamental component. A low value of current THD (2.97%) is obtained.

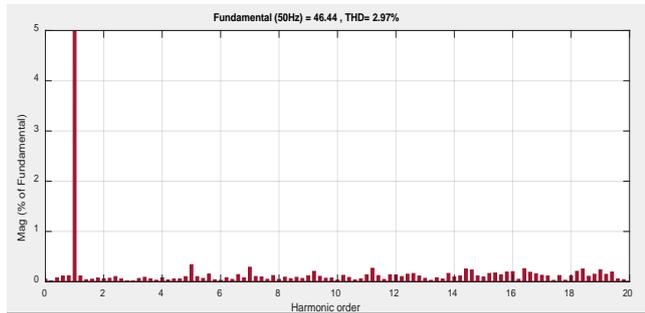


Fig. 8. Harmonic spectrum of line current.

Figure. 9 shows converter line current (i_{ca}) and its associated active and reactive powers (P_c , and Q_c). It also shows supply active and reactive powers (P_s , and Q_s) with respect to the source phase voltage. It can be noticed that converter current (i_{ca}) leads the source voltage with angle (φ_c), thus reactive power absorbed by motor is delivered from converter circuit rather than the source. In this situation, the source reactive power equals zero and converter reactive power is the negative value of motor reactive power ($-Q_c = Q$).

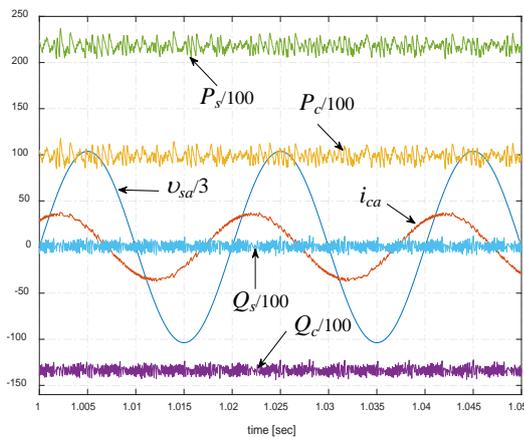


Fig. 9. System active and reactive powers.

The converter voltage (v_{ca}) and its fundamental components (v_{ca1}) are shown in figure 10 with respect to phase voltage. Referring to phasor diagram of figure 3, the waveform of v_{ca1} lags the phase voltage with an angle (δ) to verify unity power factor operation.

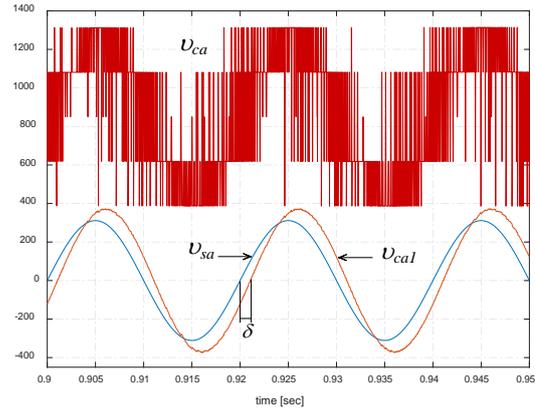


Fig. 10. Converter phase voltage and its fundamental components with respect to source voltage.

In figure 11, system quadrature currents and source direct current are presented. For lagging displacement factor of motor current, the quadrature component is negative (i_{lq}) and this current is compensated by the same positive value generated by the converter current (i_{cq}). Hence the quadrature source current (i_{sq}) has zero value, which indicates zero reactive power delivered by source voltage.

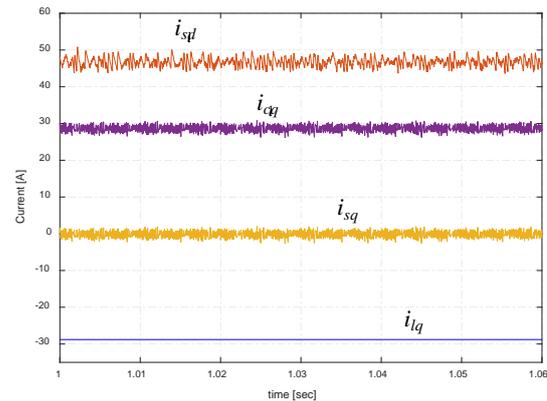


Fig. 11. Quadrature components of system currents.

Figure. 12 presents the response of PWM rectifier according to 18.75% step change in DC reference voltage. It is seen that the response of DC voltage to a sudden change in its reference value has a fast response (within a quarter cycle). In addition, the reactive power compensation effectively functioned where ($-i_{cq} = i_{lq}$) and ($i_{sq} = zero$).

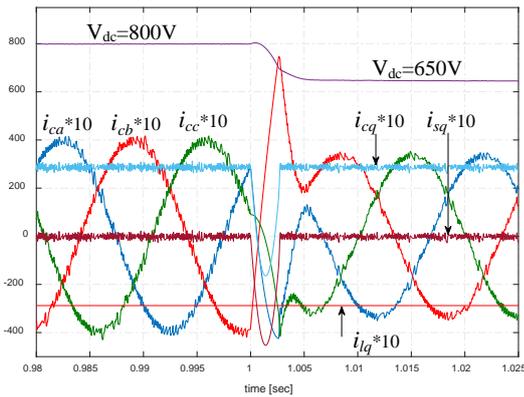


Fig. 12. Transient response of PWM rectifier according to step change in DC output voltage.

5 Experimental Setup and Results

The prototype of three-phase PWM rectifier system is presented in figure 13. This system requires four current sensors, two of them required for measuring motor currents and the others for converter currents. In addition, a voltage sensor is required for measuring the DC output voltage. Thus, the selected microcontroller should have at least five A/D converter channels to adopt these measurements.

The proposed algorithm is carried out using a high speed 80C196KC microcontroller, and software code is written by assembly machine language to maximize the performance of microcontroller. Operation of PWM rectifier requires a synchronization between control circuit and AC power frequency. This function is accomplished by generating a square wave at power frequency and capturing its rising edges using the speed input unit (HSI). This unit is built in microcontroller. A unity sine-wave is generated each rising edge of synchronizing signal to provide PLL circuit. In addition, five A/D channels are used for reading measured current and voltage signals, whereas the switching signals required by IGBT's drive circuit are generated by digital output ports of microcontroller. According to large no. of A/D channels used, the lowest sample time can be obtained is 200µs. In practical experiments, a lightly loaded, 1-hp, three-phase induction motor is connected to PCC to realize a poor power factor inductive load.

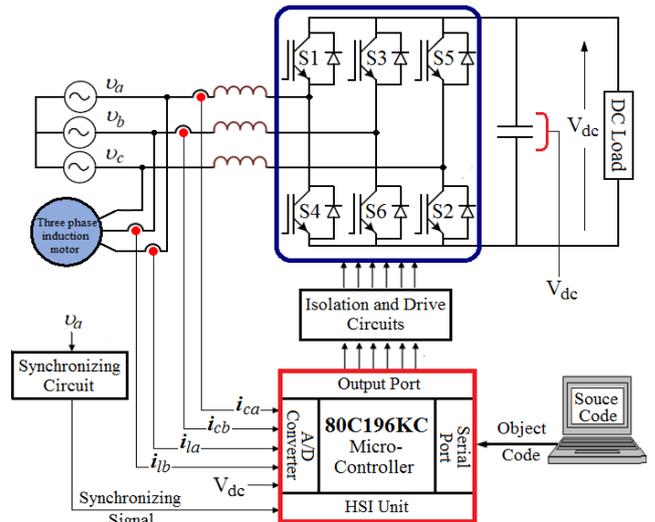


Fig. 13. Setup of experimental prototype.

Figure. 14 shows the waveform of line current with respect to phase voltage according to conventional three-phase diode bridge rectifier. The line current waveform is highly distorted and draws reactive power components. Figure. 15 presents the harmonic spectrum of line current, which determines that current waveform is highly distorted and has THD value of 22%.

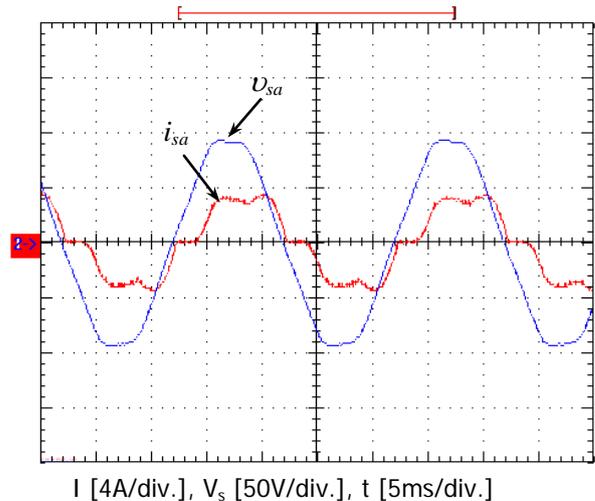


Fig. 14. Steady state performance of three-phase bridge diode rectifier.

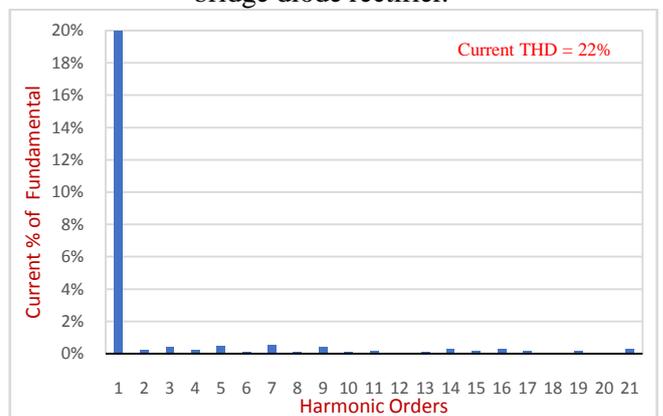
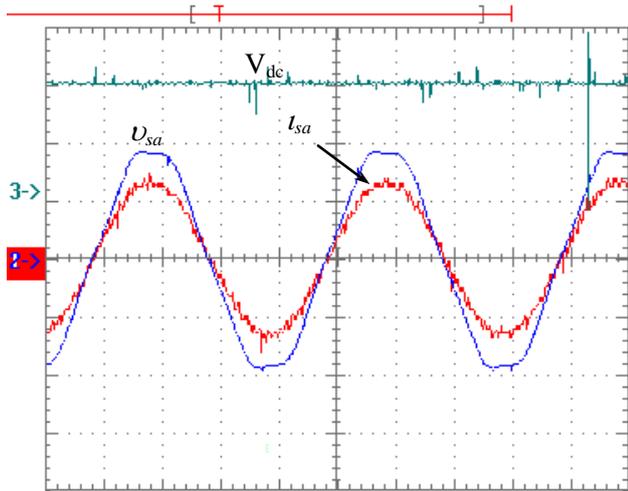


Fig. 15. Harmonic spectrum of line current drawn by three-phase bridge diode rectifier

Figure. 16 shows the performance of the PWM rectifier without connecting the motor as inductive load. The line current appears sinusoidal with a low THD value of 2.6% as indicated in figure 17. The dc output voltage is regulated at its predetermined value of 180V.



I [4A/div.], V_s [50V/div.], V_{dc} [100V/div.] t [5ms/div.]
Fig.17. Steady state performance of PWM rectifier.

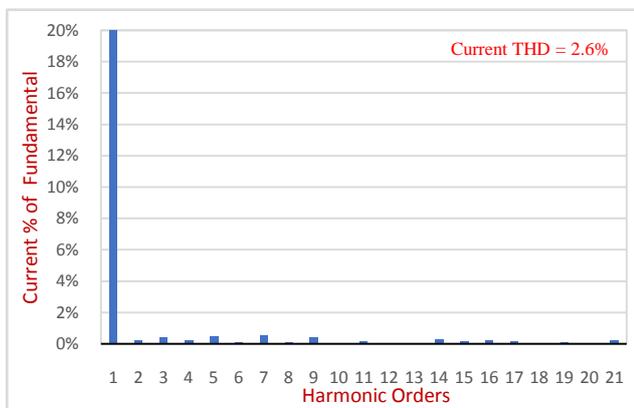
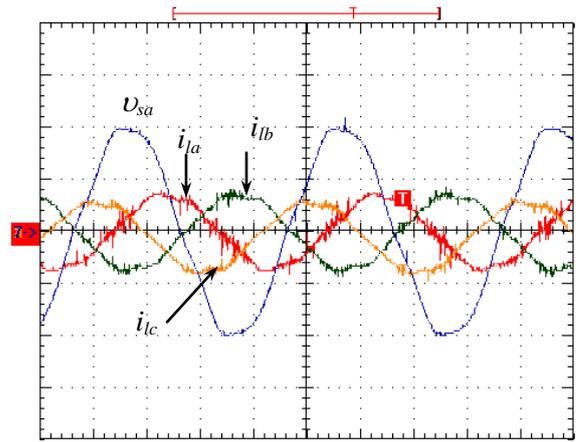


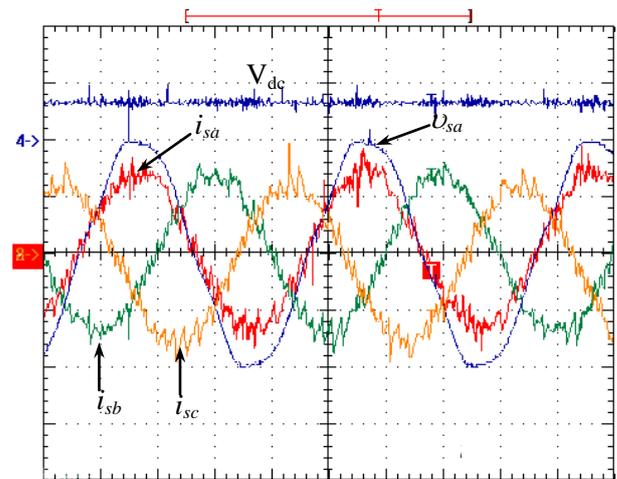
Fig. 17. Harmonic spectrum of line current drawn by three-phase PWM rectifier

Figure. 18 presents the three phase motor currents with respect to mains phase voltage. It can be observed that motor current lags the phase voltage with a relatively large angle, which indicates the poor power factor of motor operation especially when driving low mechanical loads.



I [4A/div.], V_s [50V/div.], t [5ms/div.]
Fig. 18. Three-phase motor line currents and source voltage.

The performance of the PWM rectifier with function of reactive power compensation is shown in figure 19. It is seen that the three-phase line currents are near sinusoidal and in phase with supply voltage, which indicates that overall power factor is near unity. Thus, function of reactive power compensation is effectively operating. In addition, DC output voltage is regulated at its reference value of 180V.



I [2A/div.], V_s [50V/div.], V_{dc} [300V/div.] t [5ms/div.]
Fig. 19. Performance of PWM rectifier according to reactive power compensations.

Figure 20 present the harmonic spectrum of supply current after harmonics and power factor compensation. The mains current has a low THD value of 4.23%, which meets the international harmonic standards.

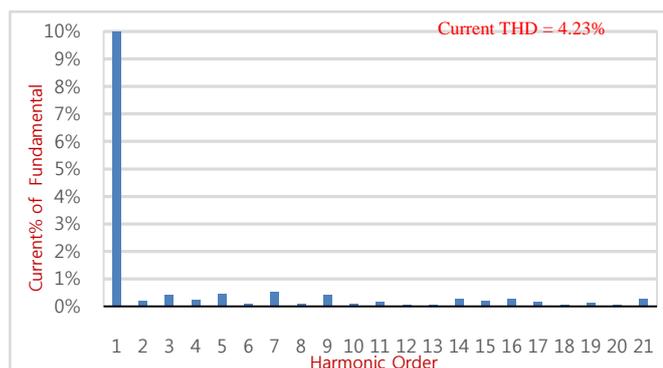


Fig. 20. Harmonic spectrum of mains current.

6 Conclusion

This paper proposes a power factor compensation as an additional function of PWM rectifier for low power factor inductive loads such as three phase induction motors connected to same PCC. The proposed control strategy is based on application of dq theory for both load current and converter current to compensate for low loads displacement factor and line current harmonics. A PI-controller is used to adjust and regulate the DC output voltage, while an LPF is used to extract the harmonic contents from direct components of line current. The control algorithm is accomplished by a single-chip low-cost 80C196KC microcontroller, by which software program is written in assembly language to maximize controller performance. The lowest sampling time obtained is $200\mu\text{s}$ which gives an approximated average switching frequency of 1KHz. The simulation and experimental results are taken at different operating condition to prove effectively that PWM converter delivers reactive power required by induction motor rather than supply and waveform of line current is near sinusoidal with low THD value of 4.23%.

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