

# Soret and Dufour Effects on Natural Convection Heat and Mass Transfer Flow past a Horizontal Surface in a Porous Medium with Variable Viscosity

M. B. K. MOORTHY  
 Department of Mathematics  
 Institute of Road and Transport Technology  
 Erode -638316, Tamilnadu  
 INDIA.

T. KANNAN and K. SENTHILVADIVU  
 Department of Mathematics,  
 K.S.Rangasamy College of Technology,  
 Tiruchengode -637215, Tamilnadu  
 INDIA  
 E-mail:tkannanmat@gmail.com

*Abstract:* - The heat and mass transfer characteristics of natural convection about a horizontal surface embedded in a saturated porous medium subject to variable viscosity are numerically analyzed, by taking into account the diffusion-thermo (Dufour) and thermal-diffusion (Soret) effects. The governing equations of continuity, momentum, energy and concentration are transformed into non-linear ordinary differential equations, using similarity transformations and then solved by using Runge-Kutta-Gill method along with shooting technique. The governing parameters of the problem are variable viscosity ( $\theta_c$ ), buoyancy ratio (N), Lewis number (Le), Prandtl number (Pr), Dufour number, Soret number and Schmidt number. The velocity, temperature and concentration distributions are presented graphically. The Nusselt number and Sherwood number are also derived and discussed numerically.

*Key-Words:* - Heat and Mass transfer, Natural convection, Variable viscosity, Dufour and Soret effects.

## 1 Introduction

Coupled heat and mass transfer by natural convection in a fluid saturated porous medium has received great attention during the last decades due to the importance of this process which occurs in many engineering, geophysical and natural systems of practical interest such as geothermal energy utilization, thermal energy storage and recoverable systems and petroleum reservoirs. A comprehensive account of the available information in this field is provided in recent books by Pop and Ingham [11], Ingham and Pop [12] and Vafai [13].

The previous studies, dealing with the transport phenomena of momentum and heat transfer, have dealt with one component phases which possess a natural tendency to reach equilibrium conditions. However, there are activities, especially in industrial and chemical engineering processes, where a system contains two or more components whose concentrations vary from point to point. In such a system there is a natural tendency for mass to be transferred, minimizing the concentration differences within the system and the transport of

one constituent, from a region of higher concentration to that of a lower concentration. This is called mass transfer.

When heat and mass transfer occurs simultaneously between the fluxes, the driving potential is of more intricate nature, as energy flux can be generated not only by temperature gradients but by composition gradients as well. The energy flux caused by a composition gradient is called the Dufour or diffusion-thermo effect. Temperature gradients can also create mass fluxes, and this is the Soret or thermal-diffusion effect. Generally, the thermal-diffusion and the diffusion-thermo effects are of smaller order magnitude than the effects prescribed by Fourier's or Fick's laws and are often neglected in heat and mass transfer processes. There are, however, exceptions. The Soret effect, for instance, has been utilized for isotope separation, and in mixtures between gases with very light molecular weight (H<sub>2</sub>, He). For medium molecular weight (N<sub>2</sub>, air), the Dufour effect was found to be of a considerable magnitude such that it cannot be neglected (Eckert and Drake) [1].

Kassoy and Zebib [2] studied the effect of variable viscosity on the onset of convection in porous medium. Cheng and Minkowycz [3] studied the effect of free convection about a vertical plate embedded in a porous medium with application to heat transfer from a dike. Chang and Cheng [4] studied the matched asymptotic expansion for free convection about an impermeable horizontal surface in a porous medium. Bejan and Khair [5] studied the buoyancy induced heat and mass transfer from a vertical plate embedded in a saturated porous medium. Rami. Y. Jumah et al. [7] studied the coupled heat and mass transfer for non-Newtonian fluids. Anghel et al [8] investigated the Dufour and Soret effects on free convection boundary layer over a vertical surface embedded in a porous medium. Kumari [9] analyzed the effect of variable viscosity on free and mixed convection boundary layer flow from a horizontal surface in a saturated porous medium. Postelnicu et al. [10] investigated the effect of variable viscosity on forced convection over a horizontal flat plate in a porous medium with internal heat generation. Seddeek [14, 15] studied the effects of chemical reaction, variable viscosity, and thermal diffusivity on mixed convection heat and mass transfer through porous media. Mohamed E- Ali [16] studied the effect of variable viscosity on mixed convection along a vertical plate. Alam et al [17] analyzed the study of the combined free - forced convection and mass transfer flow past a vertical porous plate in a porous medium with heat generation and thermal diffusion. Pantokratoras [18] analyzed the effect of variable viscosity with constant wall temperature. Partha et al [19] analyzed Soret and Dufour effects in non-Darcy porous medium. Alam and Rahman [20] studied the Dufour and Soret effects on mixed convective flow past a vertical porous plate with variable suction. Seddeek et al [21] studied the effects of chemical reaction and variable viscosity on hydro magnetic mixed convection heat and mass transfer through porous media. Another contribution to the theme of Dufour and Soret effects can be found in the paper by Afify [22], where there is a non-Darcy free convection past a vertical surface with temperature viscosity. Lakshmi Narayana and Murthy [23] studied the Soret and Dufour effects on free convection heat and mass transfer from a horizontal flat plate in a Darcy porous medium. Postelnicu [24] studied the influence of chemical reaction along with Soret and Dufour effects in the absence of magnetic field on free convection. Bansod and Jadhav [25] studied an integral treatment for combined heat and mass transfer by natural convection along a horizontal surface in a porous medium. El-Arabawy [26]

studied the Soret and Dufour effects in a vertical plate with variable surface temperature. Postelnicu [27] analyzed the effect of Soret and Dufour on heat and mass transfer at a stagnation point. Tak et al [28] investigated the MHD free convection- radiation in the presence of Soret and Dufour. Vempati et al [29] studied the Soret and Dufour on MHD with thermal radiation. Ching-Yang Cheng [30] studied the Soret and Dufour on heat and mass transfer on a vertical truncated cone with variable wall temperature and concentration. The authors [31] studied variable viscosity on convective heat and mass transfer by natural convection from horizontal surface in porous medium. Recently the same authors [32] studied Soret and Dufour effects on natural convection flow past a vertical surface in a porous medium with variable viscosity. Apart from the existence, survey of literature was taken into account with respect to the effects of (i) thermal stratification (ii) variable viscosity (iii) Dufour and Soret (which is a major factor). The effects of these parameters on heat and mass transfer are discussed elaborately. In particular, the Dufour and Soret effects have the major role in our findings. Therefore, the aim of this paper is to study the effects of Soret and Dufour on heat and mass transfer by natural convection from a horizontal plate with variable viscosity.

## 2 Mathematical Model

Consider a horizontal surface embedded in a saturated porous medium. The properties of the fluid and porous medium are isotropic and the viscosity of the fluid is assumed to be an inverse linear function of temperature. Using Boussinesq and boundary layer approximations, the governing equations of continuity, momentum, energy and concentration are given by

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (1)$$

$$u = -\frac{\kappa}{\mu} \left( \frac{\partial p}{\partial x} \right) \quad (2)$$

$$v = -\frac{\kappa}{\mu} \left( \frac{\partial p}{\partial y} + \rho g \right) \quad (3)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha \frac{\partial^2 T}{\partial y^2} + \frac{D_m k_T}{c_s c_p} \frac{\partial^2 c}{\partial y^2} \quad (4)$$

$$u \frac{\partial c}{\partial x} + v \frac{\partial c}{\partial y} = D_m \frac{\partial^2 c}{\partial y^2} + \frac{D_m k_T}{T_m} \frac{\partial^2 T}{\partial y^2} \quad (5)$$

and with the Boussinesq approximation

$$\rho = \rho_\infty \{1 - \beta(T - T_\infty) - \beta^*(c - c_\infty)\} \quad (6)$$

The viscosity of the fluid is assumed to be an inverse linear function of temperature and it can be expressed as

$$\frac{1}{\mu} = \frac{1}{\mu_\infty} \{1 + \gamma(T - T_\infty)\} \quad (7)$$

which is reasonable for liquids such as water and oil. Here  $\gamma$  is a constant. The boundary conditions are

$$y = 0, v = 0, T = T_w, c = c_w \quad (8)$$

$$y \rightarrow \infty, u = 0, T = T_\infty, c = c_\infty \quad (9)$$

### 3 Method of Solution

Introducing the stream function  $\psi(x, y)$  such that

$$u = \frac{\partial \psi}{\partial y}, v = -\frac{\partial \psi}{\partial x} \quad (10)$$

where

$$\psi = \alpha f (Ra_x)^{1/3} \quad (11)$$

$$\eta = \frac{y}{x} (Ra_x)^{1/3} \quad (12)$$

and

$$Ra_x = \left\{ \frac{kg\beta\Delta T x}{\nu\alpha} \right\} \text{ is the Rayleigh number}$$

Define

$$\theta = \frac{T - T_\infty}{T_w - T_\infty} \quad (13)$$

$$\phi = \frac{c - c_\infty}{c_w - c_\infty} \quad (14)$$

and

$$N = \frac{\beta^*(c_w - c_\infty)}{\beta(T_w - T_\infty)} \quad (15)$$

Substitution of these transformations (10) to (15) to equations (2) to (5) along with the equations (6) and (7), the resulting nonlinear ordinary differential equations are

$$f'' = \frac{f'\theta'}{\theta - \theta_c} - \frac{2}{3} \left( \frac{\theta - \theta_c}{\theta_c} \right) (\eta\theta' + \eta\phi'N) \quad (16)$$

$$\theta'' + Pr Du\phi'' + \frac{1}{3} f\theta' = 0 \quad (17)$$

$$\phi'' + S_c S_r \theta'' + \frac{Le}{3} f\phi' = 0 \quad (18)$$

together with the boundary conditions

$$\eta = 0, f = 0, \theta = 1, \phi = 1 \quad (19)$$

$$\eta \rightarrow \infty, f' = 0, \theta = 0, \phi = 0 \quad (20)$$

where  $Pr = \frac{\nu}{\alpha}$  is the Prandtl number,

$Du = \frac{D_m k_T (c_w - c_\infty)}{c_s c_p \nu (T_w - T_\infty)}$  is the Dufour number,

$S_c = \frac{\nu}{D_m}$  is the Schmidt number,

$S_r = \frac{D_m k_T (T_w - T_\infty)}{T_m \nu (c_w - c_\infty)}$  is the Soret number  $Le = \frac{\alpha}{D_m}$

is the Lewis number and  $\theta_c = -\frac{1}{\gamma}(T_w - T_\infty)$  is the parameter characterizing the influence of viscosity. For a given temperature difference, large values of  $\theta_c$  implies either  $\gamma$  or  $(T_w - T_\infty)$  are small. In this case, the effect of variable viscosity can be neglected.

The effect of variable viscosity is important if  $\theta_c$  is small. Since the viscosity of liquids decreases with increasing temperature while it increases for gases,  $\theta_c$  is negative for liquids and positive for gases. The concept of this parameter  $\theta_c$  was first introduced by Ling and Dybbs [6] in their study of forced convection flow in porous media. The parameter N measures the relative importance of mass and thermal diffusion in the buoyancy-driven flow. It is clear that N is zero for thermal-driven flow, infinite for mass driven flow, positive for aiding flow and negative for opposing flow.

### 4 Numerical analysis and Discussion

The equations (16), (17) and (18) together with the boundary conditions (19) and (20) are integrated numerically by using the fourth order Runge-Kutta-Gill method along with a systematic guessing of  $-\theta'(0)$  and  $-\phi'(0)$  by the shooting technique. The step size  $\Delta\eta=0.0625$  is used to obtain the numerical solution with seven decimal place accuracy as the criterion of convergence.

The parameters involved in this problem are  $\theta_c$  – the variable viscosity,  $Le$ - Lewis number ,  $N$ -the buoyancy parameter,  $Pr$ - Prandtl number,  $Du$ - Dufour number,  $Sr$ - Soret number and  $Sc$ - Schmidt number. To observe the effect of variable viscosity on heat and mass transfer we have plotted the velocity function  $f'$  , temperature function  $\theta$  and the concentration function  $\phi$  against  $\eta$  for various values of  $\theta_c$ ,  $Le$  and  $N$ . The value of Prandtl number  $Pr$  is taken equal to 0.71 which corresponds to air. The values of the Dufour number and Soret number are taken in such a way that their product is constant according to their definition provided that the mean temperature is kept constant as well. The parameter  $\theta_c$  is used to represent the effect of variable viscosity. The case  $\theta_c < 0$  corresponds to the case of liquids and  $\theta_c > 0$  corresponds to the case of gases.

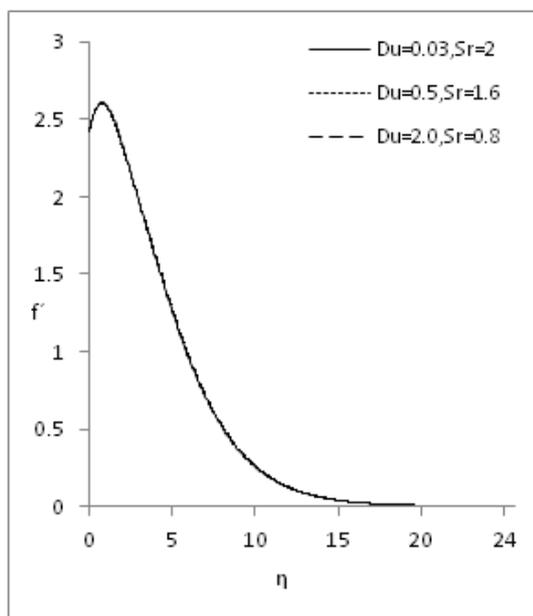


Fig.1: Velocity profile for different values of Dufour and Soret for  $\theta_c=5$ ,  $N=1$ ,  $Le=0.1$ ,  $Pr=0.71$  and  $Sc=0.1$ .

The influence of Dufour number  $Du$  and Soret number  $Sr$  on velocity, temperature and concentration profiles are shown in Figs.1,2 and 3 respectively for  $\theta_c= 5$ ,  $N=1$ ,  $Le=0.1$ ,  $Pr=0.71$  and  $Sc=0.1$ . Fig.1 shows that the velocity decreases slightly with the increase of Dufour number whereas it decreases with the decrease of Soret number.

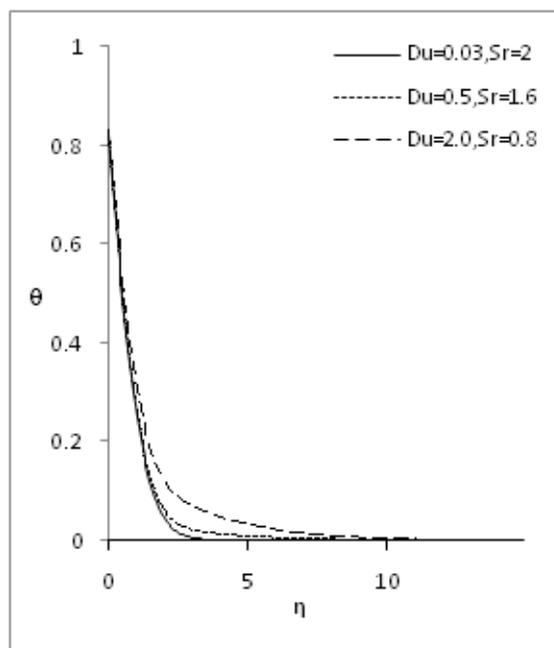


Fig.2: Temperature profile for different values of Dufour and Soret for  $\theta_c=5$ ,  $N=1$ ,  $Le=0.1$ ,  $Pr=0.71$  and  $Sc=0.1$ .

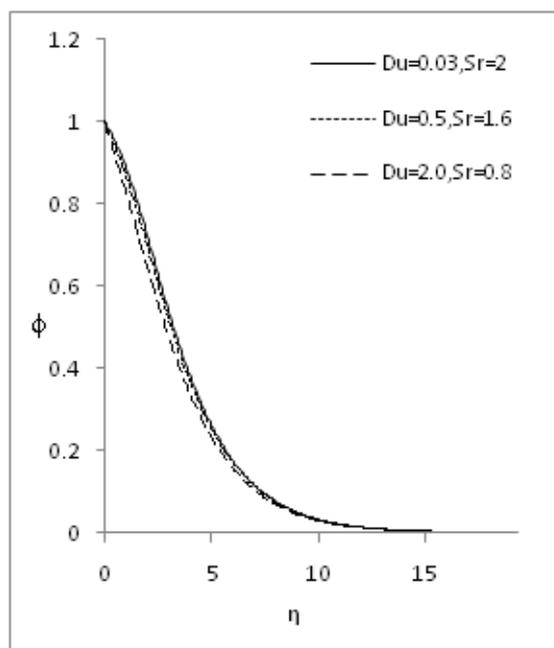


Fig.3: Concentration profile for different values of Dufour and Soret for  $\theta_c=5$ ,  $N=1$ ,  $Le=0.1$ ,  $Pr=0.71$  and  $Sc=0.1$ .

Fig. 3 shows that the concentration decreases with the increase of Dufour number whereas it increases with the increase of Soret number.

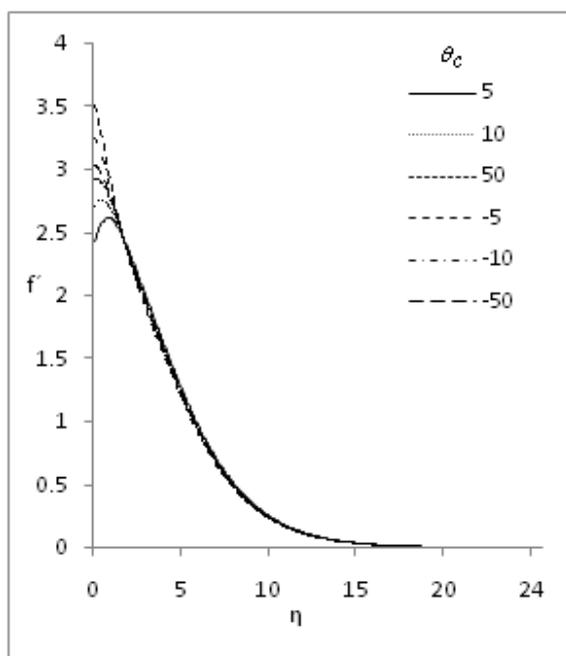


Fig.4: Velocity profile for different values of  $\theta_c$  for  $Du=0.03$ ,  $Sr=2$ ,  $N=1$ ,  $Le=0.1$ ,  $Pr=0.71$  and  $Sc=0.1$ .

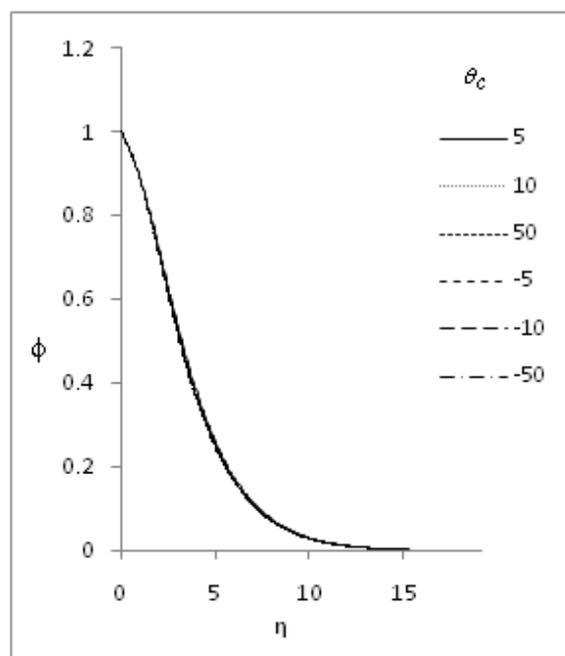


Fig.6: Concentration profile for different values of  $\theta_c$  for  $Du=0.03$ ,  $Sr=2$ ,  $N=1$ ,  $Le=0.1$ ,  $Pr=0.71$  and  $Sc=0.1$ .

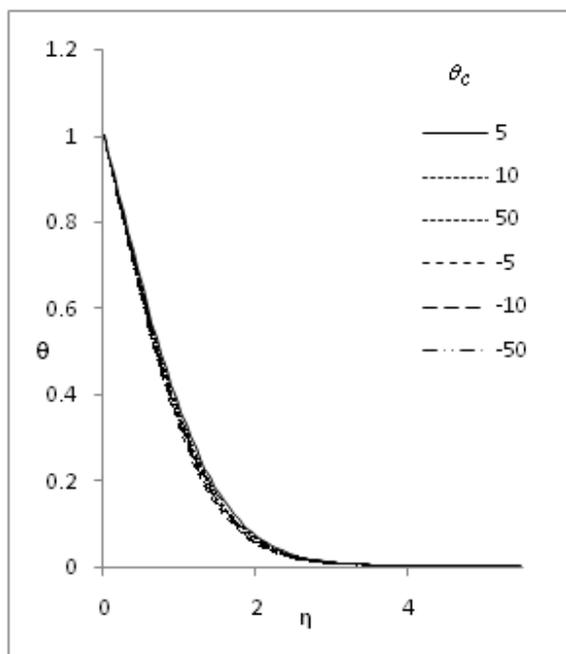


Fig.5: Temperature profile for different values of  $\theta_c$  for  $Du=0.03$ ,  $Sr=2$ ,  $N=1$ ,  $Le=0.1$ ,  $Pr=0.71$  and  $Sc=0.1$ .

The effect of variable viscosity  $\theta_c$  on velocity, temperature and concentration are shown in Figs. 4, 5 and 6 respectively for  $N=1$ ,  $Le = 0.1$ ,  $Pr = 0.71$ ,  $Sc = 0.1$ ,  $Du = 0.03$  and  $Sr = 2$ . From Fig. 4 it is realized that the velocity increases near the plate and decreases away from the plate as  $\theta_c \rightarrow 0$  in the case of liquids ( $\theta_c < 0$ ) and decreases near the plate and increases away from the plate as  $\theta_c \rightarrow 0$  in the case of gases ( $\theta_c > 0$ ). From Figs. 5 and 6 it is evident that the temperature and concentration increase as  $\theta_c \rightarrow 0$  for  $\theta_c > 0$  (i.e. for gases) and decreases as  $\theta_c \rightarrow 0$  for  $\theta_c < 0$  (i.e. for liquids).

The effect of Lewis number  $Le$  on temperature and concentration are shown in Figs.7 and 8 respectively for  $N = 1$ ,  $Pr = 0.71$ ,  $Sc = 0.1$ ,  $Du = 0.03$ ,  $Sr = 2$  and for different values of  $\theta_c$  and  $Le$ .

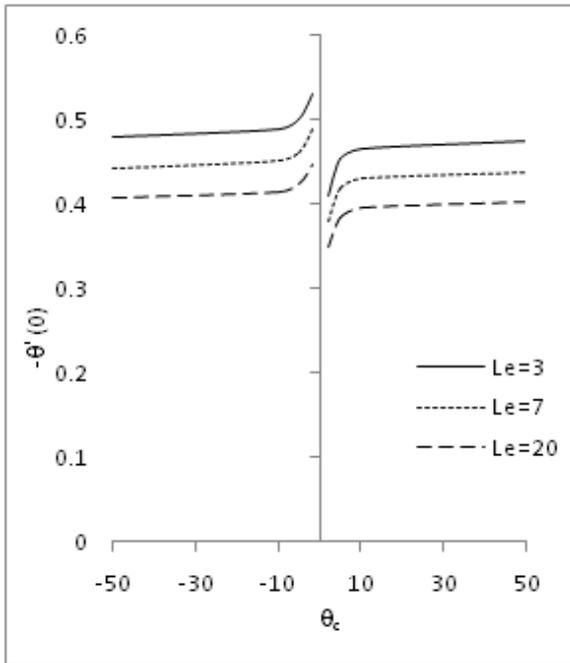


Fig.7: Effect of Lewis number  $Le$  on the rate of heat transfer for different values of  $\theta_c$ , for  $Du=0.03$ ,  $Sr=2, N=1, Pr=0.71$  and  $Sc=0.1$ .

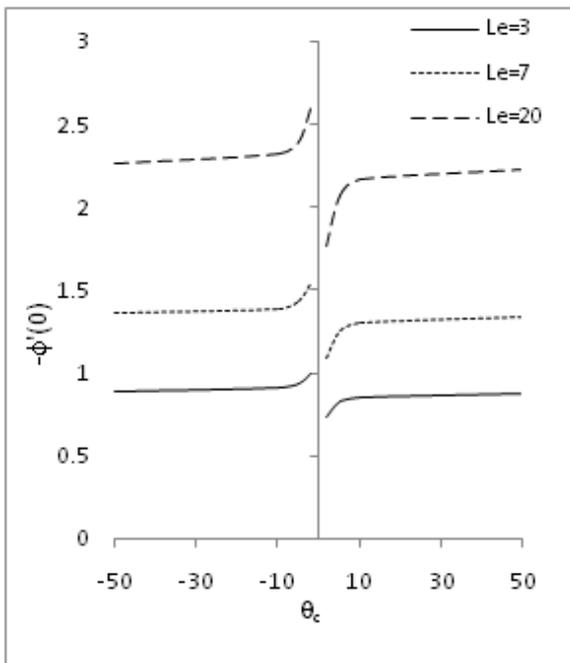


Fig.8: Effect of Lewis number  $Le$  on the rate of mass transfer for different values of  $\theta_c$ , for  $Du=0.03$ ,  $Sr=2, N=1, Pr=0.71$  and  $Sc=0.1$ .

From Fig. 7, it is observed that as  $Le$  increases, the heat transfer decreases for both gases and liquids. From Fig. 8, it is realized that as  $Le$  increases, the mass transfer increases for both gases and liquids.

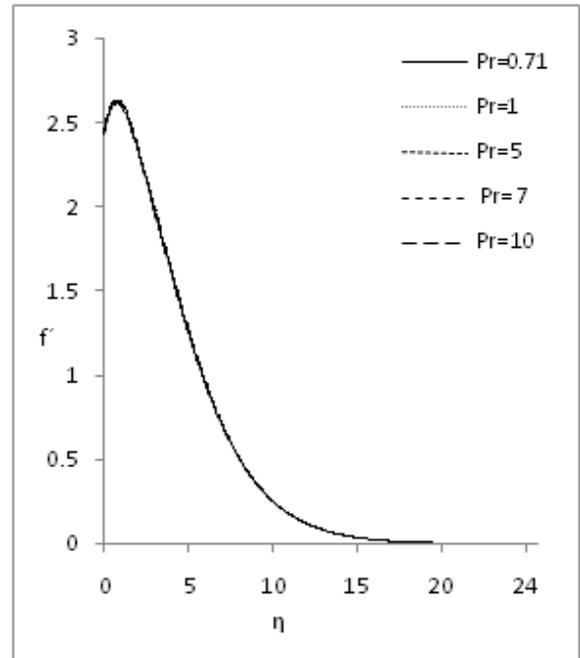


Fig.9: Velocity profile for different values of  $Pr$ , for  $Du=0.03$ ,  $Sr=2, \theta_c=5, Le=0.1, N=1$  and  $Sc=0.1$ .

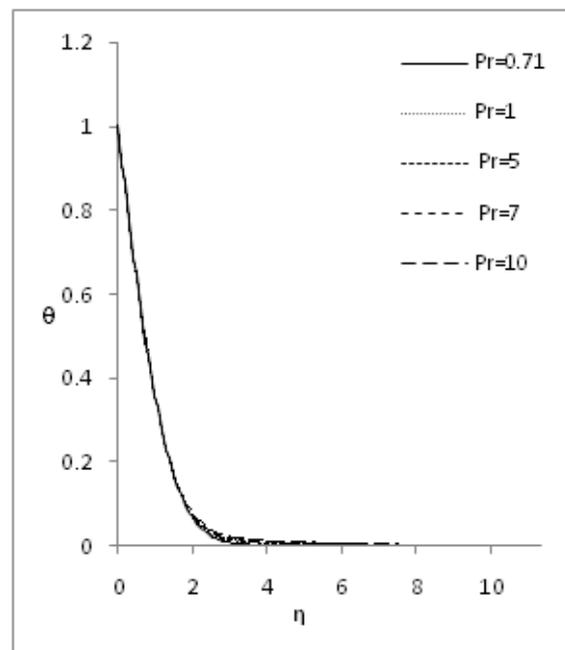


Fig.10: Temperature profile for different values of  $Pr$ , for  $Du=0.03$ ,  $Sr=2, \theta_c=5, Le=0.1, N=1$ .

The effect of Prandtl number  $Pr$  on velocity, temperature and concentration are shown in Figs. 9, 10 and 11 respectively for  $N = 1, Sc = 0.1, Du = 0.03, Sr = 2, Le = 0.1$  and  $\theta_c = 5$ . From Figs. 9 and 10, it is evident that as the Prandtl number increases, the velocity and temperature increases.

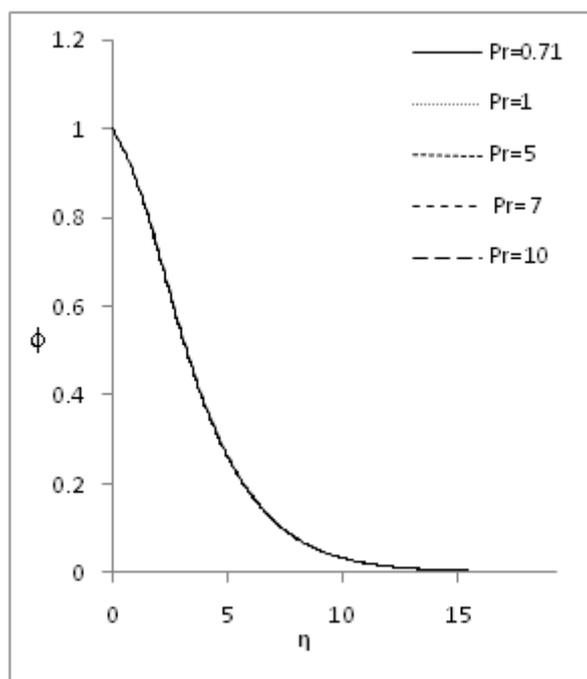


Fig.11: Concentration profile for different values of Pr, for Du=0.03, Sr=2,  $\theta_c=5$ , Le=0.1, N=1 and Sc=0.1.

Fig. 11 shows that as the Prandtl number increases, the concentration decrease.

The parameters of engineering interests for the present problem are the local Nusselt number  $Nu_x$  and Sherwood number  $Sh_x$ , which are given by

$$\frac{Nu_x}{(Ra_x)^{1/3}} = -\theta'(0) \tag{21}$$

$$\frac{Sh_x}{(Ra_x)^{1/3}} = -\phi'(0) \tag{22}$$

Table 1: Values of local Nusselt number for an isothermal plate for Le=1,N=0,M=0,Du=0,Sr=0 and  $\theta_c \rightarrow \infty$

Chang and Cheng [4]	Bansod and Jadhav [25]	Present case
0.429	0.421	0.429

Table 1 represents a comparison of the numerical values of Nusselt number obtained in the present case with those of Chang and Cheng [4] and Bansod

and Jadhav [25] for an isothermal plate for Le=1, N=0, M=0, Du=0, Sr=0 and  $\theta_c \rightarrow \infty$ . It is clearly seen that there is a good agreement between the results.

Table 2: Numerical values of Nusselt numbers for various values of N and  $\theta_c$  for Le = 0.1, Du = 0.03, Sr = 2, and Sc = 0.1.

Nusselt number			
$\theta_c$	N		
	1	2	5
5	0.7338743	0.8919685	1.1819310
10	0.7569678	0.9203725	1.2198963
50	0.7747059	0.9422032	1.2490883
-5	0.8205859	0.9987185	1.3247071
-10	0.8002210	0.9736245	1.2911228
-50	0.7833500	0.9528458	1.2633233

Table 3: Numerical values of Sherwood number for various values of N and  $\theta_c$  for Le = 0.1, Du = 0.03, Sr = 2, and Sc = 0.1.

Sherwood number			
$\theta_c$	N		
	1	2	5
5	0.0989015	0.1254325	0.1709522
10	0.0974540	0.1237351	0.1687599
50	0.0963345	0.1224187	0.1670559
-5	0.0934128	0.1189691	0.1625774
-10	0.0947139	0.1205077	0.1645771
-50	0.0957867	0.1217735	0.1662196

The values of Nusselt number and Sherwood number for different values of variable viscosity  $\theta_c$  and the buoyancy ratio N are presented in Table 2 & 3 for Le=0.1, Sc=0.1, Du=0.03,Sr = 2 and Pr = 0.71.

It is evident that as  $\theta_c \rightarrow 0$  for gases the Nusselt number decreases and the Sherwood number increases. It is also realized that as  $\theta_c \rightarrow 0$  for liquids the Nusselt number increases and the Sherwood number decreases for other parameters fixed.

## 5 Conclusion

The Dufour and Soret effect on free convective heat and mass transfer flow past a semi-infinite horizontal plate under the influence of variable viscosity has been studied. Using usual similarity transformations, the governing equations have been transformed into non-linear ordinary differential equations. The similarity solutions are obtained numerically by applying Runge-Kutta-Gill method along with shooting technique.

## Nomenclature

$c$  - Concentration at any point in the flow field  
 $c_p$  - Specific heat at constant pressure  
 $c_s$  - Concentration susceptibility  
 $c_w$  - Concentration at the wall  
 $c_\infty$  - Concentration at the free stream  
 $D_m$  - Mass diffusivity  
 $Du$  - Dufour number  
 $f$  - Dimensionless velocity function  
 $g$  - Acceleration due to gravity  
 $k$  - Permeability  
 $k_T$  - Thermal diffusion ratio  
 $Le$  - Lewis number [ $Le = \alpha / D_m$ ]  
 $N$  - Buoyancy ratio  
 $[N = \beta^* (c_w - c_\infty) / \beta (T_w - T_\infty)]$   
 $Nu_x$  - Nusselt number  
 $[Nu_x = -x(\partial T / \partial y)_{y=0} / (T_w - T_\infty)]$   
 $p$  - Pressure  
 $Pr$  - Prandtl number  
 $Ra_x$  - Rayleigh number  $Ra_x = [kg\beta\Delta T_x / \nu\alpha]$   
 $Sc$  - Schmidt number  
 $Sh_x$  - Sherwood number [ $Sh_x = mx / D(c_w - c_\infty)$ ]  
 $Sr$  - Soret number  
 $T$  - Temperature of the fluid  
 $T_w$  - Temperature of the plate  
 $T_\infty$  - Temperature of the fluid far from the plate  
 $T_m$  - Mean fluid temperature  
 $u, v$  - Velocity components in x and y direction  
 $x, y$  - Coordinate system

**Greek letters**  
 $\alpha$  - Thermal diffusivity  
 $\beta$  - Coefficient of thermal expansion

$\beta^*$  - Concentration expansion coefficient  
 $\gamma$  - Constant defined in equation (7)  
 $\eta$  - Dimensionless similarity variable  
 $\theta$  - Dimensionless temperature  
 $\theta_c$  -  $-1 / \gamma (T_w - T_\infty)$   
 $\mu$  - Viscosity [pas]  
 $\nu$  - Kinematic viscosity  
 $\rho$  - Density  
 $\phi$  - Dimensionless concentration  
 $\psi$  - Dimensionless stream function

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## References:

- [1] E. R. G. Eckert and R. M. Drake, *Analysis of heat and mass transfer*, McGraw-Hill, New York, NY, USA, 1972.
- [2] D. R. Kassoy and A. Zebib, Variable viscosity effects on the onset of convection in porous media, *Physics of Fluids*, vol. 18, no.12, pp.1649-1651, 1975.
- [3] P. Cheng and W. J. Minkowycz, Free convection about a vertical plate embedded in a porous medium with application to heat transfer from a dike, - *Journal of Geophysical Research*, vol.82, no.14, pp 2040-2044, 1977.
- [4] I. D. Chang, P. Cheng, Matched asymptotic expansions for free convection about an impermeable horizontal surface in a porous medium, *Int. J. Heat Mass Transfer*, vol. 26, pp. 163-174, 1983.
- [5] A. Bejan and K. R. Khair, Heat and mass transfer by natural convection in a porous medium, *International Journal of Heat Mass Transfer*, vol.28, no.5, pp.909-918 1985.
- [6] J. X. Ling and A. Dybbs, Forced convection over a flat plate submersed in a porous medium: variable viscosity case, in *Proceedings of the American Society of Mechanical Engineers*, New York, NY, USA, 1987, ASME paper 87 -WA/HT-23.
- [7] R. Y. Jumah and A. S. Mujumdar, Free convection heat and mass transfer of non-Newtonian power law fluids with yield stress from a

vertical flat plate in saturated porous media, *International Communications in Heat and Mass Transfer*, vol.27, no. 4, pp.485-494, 2000.

[8] M. Anghel, H. S. Takhar and I. Pop, Dufour and Soret effects on free convection boundary layer over a vertical surface embedded in a porous medium, *Studia Universitatis Babeş-Bolyai*, 2000, *Mathematica XLV*: pp. 11-22.

[9] M. Kumari, Variable viscosity effects on free and mixed convection boundary layer flow from a horizontal surface in a saturated porous medium-variable heat flux, *Mechanics Research Communications*, vol.28, no.3, pp. 339-348, 2001.

[10] A. Postelnicu, T. Grosan and I. Pop, The effect of variable viscosity on forced convection over a horizontal flat plate in a porous medium with internal heat generation, *Mechanics Research Communications*, vol.28, no.3, pp. 331-337, 2001.

[11] I. Pop and D. B. Ingham, *Convective heat transfer: Mathematical and computational modeling of viscous fluids and porous media*, Pergamon, Oxford, UK, 2001.

[12] D. B. Ingham and I. Pop, *Transport Phenomena in porous media III*, Elsevier, Oxford, 2005.

[13] K. Vafai, *Handbook of Porous media*, Taylor and Francis, New York, NY, USA, 2<sup>nd</sup> edition, 2005.

[14] M. A. Seddeek, Finite element method for the effects of chemical reaction, variable viscosity, thermophoresis and heat generation/ absorption on a boundary layer hydro magnetic flow with heat and mass transfer over a heat surface, *Acta Mechanica*, vol.177, pp.1-18, 2005.

[15] M. A. Seddeek and A. M. Salem, Laminar mixed convection adjacent to vertical continuously stretching sheet with variable viscosity and variable thermal diffusivity, *International Journal of Heat and Mass Transfer*, vol. 41, no.12, pp. 1048-1055, 2005.

[16] M. E. Ali, The effect of variable viscosity on mixed convection heat transfer along a vertical moving surface, *International Journal of thermal sciences*, vol.45, no.1, pp.60- 69, 2006.

[17] M. S. Alam, M. M. Rahman and M. A. Samad, Numerical study of the combined free-forced convection and Mass transfer flow past a vertical porous plate in a porous medium with heat generation and thermal diffusion, *Nonlinear Analysis: Modeling and Control*, vol.11, no. 4, pp. 331-343, 2006.

[18] A. Pantokratoras, The Falkner-skani flow with constant wall temperature and variable viscosity, *International Journal of thermal sciences*, vol.45, no.4, pp. 378-389, 2006.

[19] M. K. Partha, P.V. S. N. Murthy and G. P. R. Sekhar, Soret and Dufour effects in non- Darcy porous medium, *Journal of Heat Transfer*, vol.128, no.6, pp.605-610, 2006.

[20] M. S. Alam and M. M. Rahman, Dufour and Soret effects on mixed convection flow past a vertical porous flat plate with variable suction, *Nonlinear Analysis: Modeling and Control*, vol.11, no.1, pp.3-12, 2006.

[21] M. A. Seddeek, A. A. Darwish and M. S. Abdelmeguid, Effect of chemical reaction and variable viscosity on hydro magnetic mixed convection heat and mass transfer for Hiemenz flow through porous media with radiation, *Communications in Nonlinear Science and Numerical Simulation*, vol.12, pp.195- 213, 2007.

[22] A. Afify, Effects of thermal-diffusion and diffusion- thermo on non -Darcy MHD free convective heat and mass transfer past a vertical isothermal surface embedded in a porous medium with thermal dispersion and temperature- dependent viscosity, *Applied Mathematical Modelling*, vol.31, pp.1621-1634, 2007.

[23] P. A. Lakshmi Narayana , P. V. S. N. Murthy, Soret and Dufour effects on free convection heat and Mass transfer from a horizontal flat plate in a Darcy porous medium, *Journal of Heat Transfer*, vol.130, 104504-1-104504-5, 2008.

[24] A. Postelnicu, Influence of chemical reaction on heat and mass transfer by natural convection from vertical surfaces in porous media considering Soret and Dufour effects, *Heat and Mass Transfer*, vol.43, no.6, pp.595-602, 2007.

[25] V. J. Bansod, R. K. Jadhav, An integral treatment for combined heat and mass transfer by natural convection along a horizontal surface in a porous medium, *International Journal of Heat and Mass Transfer*, vol.52, pp. 2202- 2806, 2009.

[26] H. A. M. El-Arabawy, Soret and Dufour effects on natural convection flow past a vertical surface in a porous medium with variable surface temperature, *Journal of Mathematics and Statistics*, vol.5, no.3, pp.190-198, 2009.

[27] A. Postelnicu, Heat and Mass transfer by natural convection at a stagnation point in a porous medium considering Soret and Dufour effects, *Heat and Mass Transfer*, vol. 46, no.8-9, pp. 831-840, 2010.

[28] S. S. Tak, R. Mathur, R. K. Gehlot and A. Khan, MHD free convection – radiation interaction along a vertical surface embedded in a darcian porous medium in presence of Soret and Dufour's effects, *Thermal Science*, vol.14, no.1, pp.137-145, 2010.

- [29] S. R. Vempati and A. B. Laxmi-Narayana-Gari, Soret and Dufour effects on unsteady MHD flow past an infinite vertical porous plate with thermal radiation, *Applied Mathematics and Mechanics*, vol.31, no.12, pp. 1481-1496, 2010.
- [30] C. Y. Cheng, Soret and Dufour effects on heat and mass transfer by natural convection from a vertical truncated cone in a fluid – saturated porous medium with variable wall temperature and concentration, *International Communications in Heat and Mass Transfer*, vol.37, no.8, pp. 1031-1035, 2010.
- [31] M. B. K. Moorthy and K. Senthilvadivu, Effect of variable viscosity on convective heat and mass transfer by natural convection from horizontal surface in porous medium, *WSEAS Transactions on Mathematics*, vol.6, no.10, pp. 210-218, 2011.
- [32] M. B. K. Moorthy and K. Senthilvadivu, Soret and Dufour effects on natural convection flow past a vertical surface in a porous medium with variable viscosity, *Journal of Applied Mathematics*, Article ID 634806, 2012.